

MPI Derived Datatypes: Performance Expectations and Status Quo*

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ABSTRACT

We examine natural expectations on communication performance using MPI derived datatypes in comparison to the baseline, “raw” performance of communicating simple, non-contiguous data layouts. We show that common MPI libraries sometimes violate these datatype performance expectations, and discuss reasons why this happens, but also show cases where MPI libraries perform well. Our findings are in many ways surprising and disappointing. First, the performance of derived datatypes is sometimes worse than the semantically equivalent packing and unpacking using the corresponding MPI functionality. Second, the communication performance equivalence stated in the MPI standard between a single contiguous datatype and the repetition of its constituent datatype does not hold universally. Third, the heuristics that are typically employed by MPI libraries at type-commit time are insufficient to enforce natural performance guidelines, and better type normalization heuristics may have a significant performance impact. We show cases where all the MPI type constructors are necessary to achieve the expected performance for certain data layouts. We describe our benchmarking approach to verify the datatype performance guidelines, and present extensive verification results for different MPI libraries.

1. INTRODUCTION

The derived or user-defined datatype mechanism is a powerful, integral feature of MPI that enables communication of possibly structured, non-contiguous, and non-homogeneous (with different constituent basic types) application data with any of the MPI communication operations, without the need for tedious, explicit, possibly time- and space-consuming manual packing between intermediate communication buffers [9, Chapter 4].

Characterizing the expected and actual performance of MPI communication with structured, non-contiguous data is a difficult problem that has been addressed in many studies [3, 11, 14]. We extend and complement this research using a different approach. MPI derived datatypes can be viewed as a mechanism for serializing the access to non-con-

tiguous data layouts. Data elements stored non-contiguously in memory have to be sent or received in a certain order. Serialization can be, and in applications often is [4], handled manually by *packing* and *unpacking* the data via contiguous, intermediate buffers of elements of basic datatypes in the desired order, upon which MPI communication operations are then performed. Alternatively, the given non-contiguous data layout and access order can be described by a derived datatype, and the serialization is handled transparently by the MPI library implementation. There are three interrelated issues determining the performance of the data serialization and the derived datatype mechanism:

Issue 1 How expensive is it *per se* to access and serialize data stored in certain (non-)regular patterns in memory?

Issue 2 How well do specific MPI libraries handle the serialization using derived datatypes? Does the performance depend on the type of communication operation?

Issue 3 How do different derived datatype descriptions of the *same layout* affect serialization cost?

The first issue has to do with the data layout itself, and access performance is dependent on both the specific data layout, as well as on the memory system and other factors of the underlying system, and on how well the serialization can be implemented to exploit such capabilities (cache, vectorization, prefetching). Because of this essential dependence on both system capabilities and on what is possible for each particular access pattern, it does not seem possible to state system-independent expectations or guidelines *a priori* on the costs of processing and communicating structured data. Nevertheless, it is enlightening for users to have means to measure the difference in communication performance with differently structured data layouts.

The second issue focuses on the quality of the MPI implementation for accessing structured layouts. The MPI standard itself does not prescribe how the datatype mechanism has to be implemented. It does, however, interrelate communication and datatype constructors in a way that makes it possible to formulate and check concrete expectations on the performance of the derived datatype mechanism. We explain and examine such expectations in the paper.

The third issue is solely related to the quality of the MPI library. With the given MPI datatype constructors [9, Chap-

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ter 4], it is easy to see that the same layout can be described in an infinite number of ways (almost all of which are trivial and irrelevant). However, for a given application layout there are often competing, non-contrived ways of describing it. We can compare the communication performance with such different descriptions. It might be sensible to expect that an MPI library ensures that performance is more or less the same, no matter how the user chooses to describe the given layout. We will argue why this is a reasonable expectation, and discuss why it cannot be (easily) fulfilled.

We discuss benchmarking of the MPI derived datatype mechanism in an attempt to characterize both the “raw performance” of communication with structured data (Issue 1), as well as to develop means for verifying the expected performance of certain uses of the derived datatype mechanism. We focus on three different (meta) performance guidelines, previously discussed by Gropp *et al.* [3], but give more precise formulations and implementations here. We then use our benchmarks to evaluate concrete MPI libraries and systems. Our benchmarks are synthetic, but parameterized to make it possible to investigate patterns that are relevant for applications. Most of the patterns and derived datatype descriptions that are considered here are natural and deliberately quite simple. Other synthetic patterns, in part derived from applications, have been used in other studies [11, 14]. Schulz *et al.* used derived datatypes for piggybacking small headers on larger messages, and contrast the performance achieved with derived datatypes against uses of the MPI pack/unpack functionality [16].

We believe that the capability of transparently communicating structured data is a strong (and rather unique) feature of MPI. It is therefore important to ensure good and consistent performance of communication with derived datatypes. The larger purpose of this study is to prevent unrealistic performance expectations, but also to make developers and application programmers aware of concrete performance problems in given MPI libraries and systems. Much work has been done over the past decades in improving the communication performance with derived datatypes [1, 10, 12, 13, 15, 19]. For instance, it has been shown, in many different variations, that piece-wise packing of structured layouts described by derived datatypes can be performed efficiently [10, 15, 19]. This is important for efficient pipelining and overlapping of data accesses and communication. Likewise, some developments focused on exploiting the memory hierarchy [1] and the communication capabilities for strided, non-contiguous data communication [20].

Many of the experiments in this paper are concerned with Issue 1. The expectation is that MPI libraries (at the `MPI_Type_commit` operation) compute a good, internal representation of the user-specified datatype, which was termed *type normalization* [3]. In this paper, we put more emphasis on showing that a strong datatype normalization can be advantageous performance-wise. It has recently been shown that optimal type normalization of derived datatypes into tree-structured representations is possible in polynomial time, but costly [2, 6, 17]. The latter two papers show that normalization costs are moderate, if the `MPI_Type_create_struct` constructor is left out. However, as our examples will show, the normalization that is required in order to get the expected performance for certain layouts requires this constructor, even if the layout is homogeneous, i.e., it only consists of data items of the same basic datatype.

The paper is structured in two main parts. In Section 2, the focus is mostly on Issue 1, where communication performance for simple layouts described in simple ways is contrasted with performance with unstructured data. In Section 3, we formalize relative performance expectations as MPI performance guidelines [18], and use them to structure the experiments. The focus here is on different descriptions of the same simple layouts as used in the first part, and on the performance of derived datatypes versus packing and unpacking with the `MPI_Pack` and `MPI_Unpack` operations.

2. CHARACTERIZING DATATYPE PERFORMANCE

We first attempt to estimate the additional overhead (if any) in communicating non-contiguous data by comparing to the time for communicating the same amount of data from a contiguous memory buffer. In other words, the focus is on the differences in communication performance caused by different types of (non-)regular layouts, and not on the way that MPI handles such layouts. However, these concerns cannot be completely separated. We use MPI derived datatypes to describe our non-contiguous layouts, and thus do not attempt to estimate derived datatype overheads in any absolute way by comparing to any “best possible” way of copying non-contiguous data layouts between contiguous buffers (“packing and unpacking by hand”). The reasons for this are twofold. First, it is not at all obvious what the best possible way to manually pack some complex non-contiguous layout into a contiguous buffer for some specific system is. Second, such a comparison is not necessarily fair, since the derived datatype mechanism makes it possible to interact with the communication system, for instance by pipelining large non-contiguous buffers by partial packing [10, 15, 19] and/or by exploiting hardware capabilities for non-contiguous data communication. Such optimizations that are possible for the MPI implementation via the MPI derived datatype mechanism are difficult to perform at the application level.

To establish a baseline performance, we consider non-contiguous, blockwise, strided data layouts with a given serialization order of a given number of n elements (of some predefined, basic datatype corresponding to a programming language type), and measure the communication performance for different n . We consider what we think are the simplest such layouts, and use what we think are the MPI implementation friendliest (non-nested) derived datatypes to describe fixed blocks of k elements, such that the complete layouts are described by n/k successive, contiguous repetitions (count argument in the MPI operations) of these blocks. The baseline performance delivered by an MPI library is the time for communicating n contiguous elements of the same basic type. We describe the basic layouts in Section 2.2.

2.1 Communication Patterns

Derived datatypes can be used with all types of MPI communication operations, but may behave differently in different contexts. We therefore benchmark with three different types of communication operations in order to get an idea of whether this is the case. The n elements are communicated either from a contiguous buffer, or as a non-contiguous layout described by a derived datatype as outlined above. We use the following communication operations and patterns:

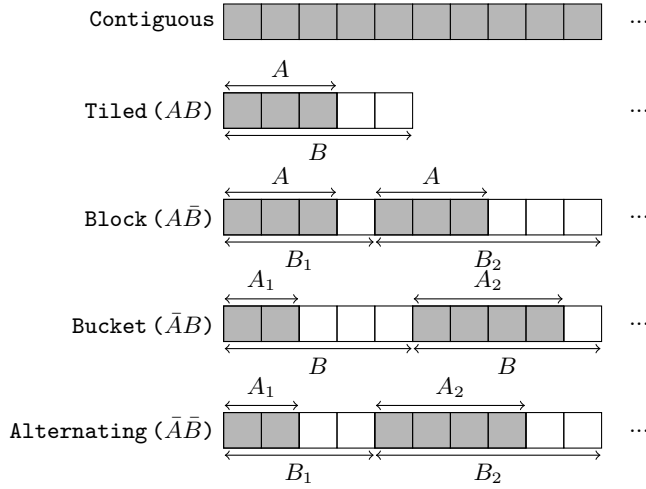


Figure 1: Basic, static layouts with parameters chosen according to **Variant 1** and with $A = 3$. Serialization of the basetype elements is from left to right.

1. *Point-to-point* communication with blocking `MPI_Send` and `MPI_Recv` operations.
2. The *asymmetric (rooted) collective* `MPI_Bcast` on p processes.
3. The *symmetric (non-rooted) collective* `MPI_Allgather` on p processes.

We do not benchmark one-sided communication performance with structured data. One reason is that with the one-sided communication model, descriptions of derived datatypes may have to be transferred between processes, and MPI libraries may differ too much in the way this is handled.

2.2 Basic, Static Datatype Layouts

We first experiment with the parameterized, blockwise layouts described below. These layouts are *static*, by which we mean that derived datatypes of k basetype elements are set up in advance and used for the whole sequence of experiments. When a total of n elements, stored according to either of these layouts, is to be communicated, the count argument in the communication operations is adjusted down to n/k . The layouts thus consist of regularly strided, but structured, non-consecutive *blocks*. We illustrate these types of blocks in Figure 1, and state below the MPI datatype constructors used to describe them. All layouts consist of contiguous smaller units of elements; we use A for the number of elements in a unit. Units are strided with some stride B , and mostly we require $B > A$. In either of the layouts the number of elements in a unit may vary (different A values), or the strides of the units may vary (different B values), or both. We use an (AB) notation for this. We use A (respectively B) when the blocksize (respectively stride) is fixed over the units, and \bar{A} (respectively \bar{B}) when the blocksize (respectively stride) varies between the units. Our basic layouts are as follows.

Contiguous: is a contiguous buffer of elements described by a predefined, basic MPI datatype (no derived datatype).

Tiled (AB) : is a contiguous unit of A elements repeated

Table 1: Hardware and software used in the experiments.

machine	36 × Dual Opteron 6134 @ 2.3 GHz
	InfiniBand QDR MT26428
machine name	<i>Jupiter</i>
MPI libraries	NEC MPI-1.3.1, MVAPICH2-2.1, OpenMPI-1.10.1
Compiler	gcc 4.4.7, gcc 4.9.2 (flags -O3)

with a stride of B elements, requirement $B > A$ (the case $B = A$ would be a contiguous layout). In MPI, the datatype is constructed using `MPI_Type_contiguous` with a count of A and a call to `MPI_Type_create_resized` to obtain the extent B . A block in this case has $k = A$ elements and an extent of B elements.

Block $(A\bar{B})$: consists of two contiguous units of A elements with alternating strides B_1 and B_2 , requirement $B_1 \neq B_2$, and $B_1, B_2 > A$ (otherwise the layout would be as above). The description in MPI is done using `MPI_Type_create_indexed_block` and `MPI_Type_create_resized`. This block has $k = 2A$ elements and an extent of $B_1 + B_2$ elements.

Bucket $(\bar{A}B)$: consists of two alternating, contiguous units of A_1 and A_2 elements, with a regular stride B , requirement $B > A_1, A_2$. The MPI description is formulated with `MPI_Type_indexed`. This block has $k = A_1 + A_2$ elements and an extent of $2B$ elements.

Alternating $(\bar{A}\bar{B})$: consists of two alternating, contiguous units of A_1 and A_2 elements, with strides B_1 and B_2 , respectively. In MPI, the datatype is described with `MPI_Type_indexed`. This block has $k = A_1 + A_2$ elements and an extent of $B_1 + B_2$ elements.

All blocks can be defined over arbitrary predefined, basic MPI datatypes. It seems natural to assume that communication performance, regardless of the type of communication, should not depend on which basic type is used, but only on the amount of data communicated. However, with MPI this assumption is problematic, since different basic types have different semantics (doubles, integers, characters), and MPI may have to handle different basic types differently. In most systems and situations, this will probably not be the case, but measurements with different basetypes have to be performed.

2.3 Benchmarking Setup

In the following, we give an overview of the hardware and software setup used for our experiments.

2.3.1 System and MPI Libraries

The experiments have been conducted on a 36 node Linux cluster called *Jupiter*, where each node is equipped with two Opteron 6134 processors (see Table 1). The nodes are interconnected using an InfiniBand QDR network. We have benchmarked the datatype performance for three MPI libraries, namely NEC MPI-1.3.1, MVAPICH2-2.1 and OpenMPI-1.10.1; in the paper we show results for the former two (see the appendix for OpenMPI-1.10.1 results). The benchmarks, for which the results are shown in the paper, have been compiled using gcc 4.4.7. We have examined the datatype performance after compiling with gcc 4.9.2, to check whether the compiler version is an experimental factor. However, we have not seen any effects by using gcc 4.9.2.

2.3.2 Benchmarking Communication Patterns

We now explain how the benchmarking of the different communication patterns was done, in particular, which times have been measured.

In each benchmark (Ping-pong or collective), we compare different datatypes for the same total communication volume. In addition, the measured run-times do not include the datatype setup times, and thus, they represent the communication times (latencies) only.

For the Ping-pong experiments, we first synchronize the two involved MPI processes with an `MPI_Barrier`. Then, a message is sent from one process, received by the other and returned using `MPI_Send` and `MPI_Recv` operations, and each process measures the time taken for the two operations. The time to perform a Ping-pong is then computed as the maximum over the local run-times of both processes. The Ping-pong measurement is repeated $nrep$ times within one `mpirun` call. Then, we repeat this Ping-pong test over r calls to `mpirun` [5]. In our Ping-pong experiments, we used $nrep = 100$ and $r = 5$.

When benchmarking the collective communication operations (`MPI_Bcast`, `MPI_Allgather`), we also synchronize the processes before each collective call with `MPI_Barrier`. All processes call the collective operation and measure the run-time (latency) locally. This measurement scheme, consisting of an `MPI_Barrier` and the timing of a collective call, is repeated $nrep$ times. The run-times (latencies) of the collective calls from each process are sent (reduced) to (on) the root process, and the run-time for a each collective call is computed as the maximum run-time over all processes. As `mpirun` can be an experimental factor, we repeat this experiment r times. For details, we refer the reader to Algorithm 1 from Hunold *et al.* [5]. Since the run-time of collective calls becomes relatively long for the larger message sizes in our experiments (e.g., around 1s for `MPI_Allgather`), we cannot afford to execute 100 repetitions for every experiment. Moreover, the variance of the run-time for such larger message sizes is relatively small. We therefore reduce the number of repetitions (of collective calls) per test case depending on the datasize m :

$$nrep = \begin{cases} 100 & \text{if } m \leq 32 \text{ kBytes,} \\ 50 & \text{if } 32 \text{ kBytes} < m \leq 320 \text{ kBytes,} \\ 20 & \text{if } m > 320 \text{ kBytes.} \end{cases}$$

Each datatype experiment with a collective call has been measured for $r = 5$ `mpiruns`.

2.3.3 Data Processing

When conducting a single datatype experiment, we obtain r datasets, each containing $nrep$ measurements. For each `mpirun`, we compute the median of the $nrep$ run-times. Then, we calculate the mean, minimum, and maximum values over these r median run-times. These values will be used in the plots, i.e., the error bars in the bar graphs denote the minimum and maximum of the r median run-times.

2.4 Experimental Results

We now summarize our findings that characterize the costs of communicating simple, structured data in comparison to communicating the same amount of contiguous data. We have used the basic datatype `MPI_INT` as the element base-type. We have experimented with two variants for each of the basic layouts, which are summarized in Table 2. All

Table 2: Basic layout variants (cf. Figure 1).

Layout	Variant 1	Variant 2
Tiled (AB)	$B = A + 2$	$B = 3A$
Block ($A\bar{B}$)	$B_1 = A + 1$ $B_2 = A + 3$	$B_1 = 2A$ $B_2 = 4A$
Bucket ($\bar{A}B$)	$A_1 = A - 1$ $A_2 = A + 1$ $B = A + 2$	$A_1 = A/2$ $A_2 = 3/2A$ $B = 3A$
Alternating ($\bar{A}\bar{B}$)	$A_1 = A - 1$ $A_2 = A + 1$ $B_1 = A + 1$ $B_2 = A + 3$	$A_1 = A/2$ $A_2 = 3/2A$ $B_1 = 2A$ $B_2 = 4A$

layouts in both variants are defined using the unit size parameter A , and the values of the A 's and B 's are chosen such that all **Variant 1** layouts have the same total extent of $n + 2n/A$, and all **Variant 2** layouts have the same total extent of $3n$.

We describe all experiments by stating the (derived) datatypes used, the reference (baseline) layout against which we evaluate, our expectations (hypotheses) on the performance, and then show and comment on the results.

This gives rise to a very large amount of experimental data, and we cannot show all our results here. A few exemplary results are included in the paper; most other results can be found in the appendix.

2.4.1 Expectation Test 1

This is our basic experiment to measure the “raw” performance of the simple, non-contiguous layouts of Figure 1. We experiment with different message sizes (fixed number of elements in the layouts) and vary the blocksize parameter A . We use both variants **Variant 1** and **Variant 2** for determining the remaining parameters in the layouts.

Experiment.

Reference Layout	Contiguous
Compared Layouts	Tiled (AB), Block ($A\bar{B}$) Bucket ($\bar{A}B$), Alternating ($\bar{A}\bar{B}$)
blocksize A	2, 10, 100, 1000, 1024, 10 000
datasize m	3200 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong, <code>MPI_Bcast</code> , <code>MPI_Allgather</code>
layout variant	1 & 2
# of processes	32×1 , 1×16 ,
(#nodes \times #cores)	(2×1 , 1×2 for Ping-pong)

Type description.

We compare the datatype layouts depicted in Figure 1.

Expectations.

We expect all communication operations with the non-contiguous layouts to be slower than using the **Contiguous** layout. We expect this difference to become smaller when increasing the blocksize A . It is interesting to find out how large the difference to the contiguous baseline performance is, how the performance is changing between the layouts, how it depends on the type of communication, and whether there are differences between the MPI libraries.

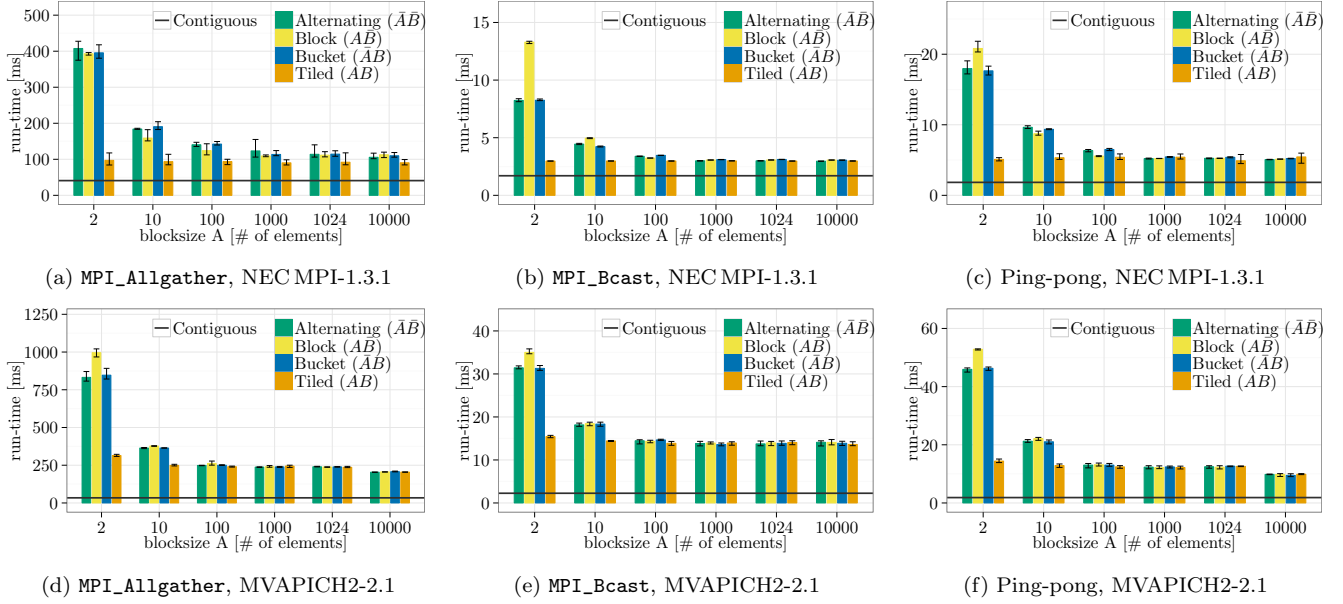


Figure 2: Contiguous vs. typed, $m = 2.56 \text{ MBytes}$, element datatype: `MPI_INT`, 32×1 processes (2×1 for Ping-pong), **Variant 1**.

Results.

The tiled layout indeed gives the best performance among the four non-contiguous layouts for all three communication patterns. The differences between the layouts are the largest for small values of the blocksize parameter A . For all libraries, there is a large difference between process configurations when all MPI processes are on the same node and when they are on different nodes (not shown here, see appendix). For the NEC MPI-1.3.1 library, the performance with non-contiguous data, especially `Tiled (AB)`, for processes on the same node is close to the raw performance with contiguous data. The libraries show a large difference in the way they handle non-contiguous data. While the raw performance with contiguous data is comparable among libraries, there is about a factor of two (and more) difference for the non-contiguous layouts, see Figure 2. The NEC MPI-1.3.1 library performs best, as it handles non-contiguous layouts with a tolerable overhead.

2.4.2 Expectation Test 2

MPI provides predefined, basic datatypes corresponding to the basic C and Fortran programming language types. These basic types have different semantic content, and communication performance may differ for data of different basic types. Knowing when this is the case is a valuable information to the application programmer. In particular, we investigate how consecutive buffers consisting of different semantic units perform in comparison to raw, uninterpreted bytes (described by `MPI_BYTE`).

Experiment.

Reference Layout	Contiguous buffer of <code>MPI_BYTE</code>
Compared Layout	Tiled-heterogeneous ($AB\bar{T}$)
blocksize A	2, 6, 8, 10, 16, 100, 128, 200
stride B	A
datasize m	48 000 Bytes, 1 500 000 Bytes
comm. patterns	Ping-pong
layout variant	1
# of processes	2×1 , 1×2

Type description.

The unit of the **Tiled-heterogeneous ($AB\bar{T}$)** layout consists of different basetypes T_1, T_2, \dots with blocksize A and stride B , where the stride of each block is given in units of the corresponding basetype. The layout is shown in Figure 3. The unit can be described in MPI using `MPI_Type_create_struct`. It is required that $B \geq A$, where equality is allowed. In our experiments, we use a contiguous layout consisting of `MPI_CHAR`, `MPI_INT`, `MPI_DOUBLE`, `MPI_SHORT`, with $B = A$ and with A varying between 2 and 200.

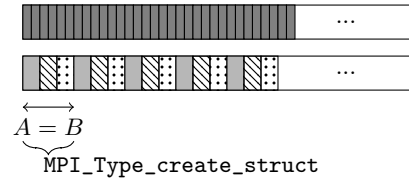


Figure 3: Contiguous buffer of bytes (`MPI_BYTE`) (top) vs. **Tiled-heterogeneous ($AB\bar{T}$)**, T_1, T_2, \dots (bottom).

Expectation.

Unless the underlying system indeed requires a different handling of different basic datatypes, we would expect that

a contiguous, dense layout of different basic types performs as well as the corresponding amount of unstructured bytes in the MPI communication operations. Since the `MPI_Type_create_struct` constructor respects alignment constraints for the basic MPI datatypes (in a sense, these are semantic constraints), there might be differences when calling `MPI_Type_create_struct` to set up the `Tiled-heterogeneous` layout leads to a non-contiguous layout. This may degrade communication performance.

Results.

Our results confirm the hypothesis. The cases with a large difference between the reference and the compared layouts can be explained by alignment constraints that cause the `Tiled-heterogeneous` layout to become larger than expected, and non-contiguous. This is the same for all three libraries. As the results are not surprising, the corresponding figures are omitted.

2.5 Summary

Our basic layouts can be used to gain insight about the performance when communicating non-contiguous data. We used only two blocksize and stride variants (see Table 2), and observed that the qualitative performance differences are similar. It may thus not be required to check a very large number of other variants. For this reason, we only use the **Variation 1** layouts in the next section. It is noteworthy that there are surprisingly large performance differences in handling structured data between the MPI libraries.

3. PERFORMANCE EXPECTATIONS

We now investigate relative performance gains (or the opposite) by using MPI derived datatypes, that is, the second and third issue raised in Section 1. We first formulate more precisely what it is reasonable to expect, and benchmark with the aim of verifying or falsifying these expectations. Our expectations take the form of self-consistent performance guidelines [18].

An MPI performance guideline states that a certain MPI operation for some given problem size n should not be slower than some equivalent MPI way of performing the same operation on the same problem size (with all other things being equal). If the MPI operation is slower than the composition of other MPI constructs implementing the same functionality, the operation could be replaced. This is clearly something that an application programmer should not have to do. Verifying such guidelines that interrelate different operations and features of the MPI standard provides a strong means of verifying that a given MPI implementation is “sane”. The verification of a set of guidelines can give valuable hints to the application programmer on how to use features of the MPI standard best.

For MPI datatypes, it seems impossible to say anything absolute about the communication performance for different layouts. But it may well be possible to formulate expectations about how the *same* layout is handled when it is described with different datatype constructors and different MPI operations.

A first guideline, which is directly derived from the MPI standard [9, Section 4.1.11], states that

$$\text{MPI}_X(c, t) \simeq \text{MPI}_X(1, \text{contig}(c, t)) \quad (\text{GL1})$$

excluding the time for setting up and committing the con-

tiguous type on the right-hand side, i.e., an MPI communication operation X should have a similar latency when transferring either c elements of type t or one derived datatype of a contiguous block of c elements. If either side of the equation would be faster than the other, the application programmer could easily switch between them. Thus, it can be expected that an MPI implementation delivers similar performance for both equation sides. As we will see, the argument is not correct, since the `MPI_Type_commit` operation can perform global optimizations on the contiguous representation of the layout that may lead to a better performance than possible with c repetitions of the block described by t . Since this cannot be controlled (or queried) by the application, the two sides of Guideline (GL1) may actually be doing different things.

The next guidelines state that whatever implicit packing and unpacking of non-contiguous data (that may be necessary inside an MPI communication operation) is performed at least as efficiently as explicitly packing and unpacking the whole communication buffer before and after the communication operation using `MPI_Pack` and `MPI_Unpack` [9, Section 4.2]. In a good MPI library, we would expect many cases when the left-hand side performs significantly better than the right-hand side. Thus:

$$\begin{aligned} \text{MPI}_X(c, t) &\preceq \text{MPI_Pack}(c, t) + \\ &\quad \text{MPI}_X(1, \text{packed}(c, t)) \end{aligned} \quad (\text{GL2})$$

for an MPI sending operation X , meaning that the performance of the left-hand side is expected to be at least as good as the performance of the right-hand side (all other things being equal). Similarly for an MPI receiving operation Y :

$$\begin{aligned} \text{MPI}_Y(c, t) &\preceq \text{MPI}_Y(1, \text{packed}(c, t)) + \\ &\quad \text{MPI_Unpack}(c, t) \end{aligned} \quad (\text{GL3})$$

The right-hand sides have the disadvantages (1) of requiring an extra buffer for the intermediate, contiguous packing unit, (2) of preventing direct communication of large contiguous parts of the datatype and (3) of preventing pipelining of packing and unpacking in the communication operations (as well as all other dynamic optimizations, and optimizations that exploit communication hardware support). Therefore it should not be recommended. We would expect that MPI libraries trivially fulfill these guidelines with equality, and would hope to find relevant cases where the left-hand sides are much faster than the right-hand sides.

Any data layout can be described in an infinite number of ways with the available MPI datatype constructors. This is easy to see, for instance `contig(1, t)` describes the same layout as t itself for any datatype t . For any given data layout, each MPI library will have layout descriptions that lead to the best communication performance. The `MPI_Type_commit` operation provides a handle for the MPI library to transform the datatype given by the user into a better (if possible), internal description. This process is called *datatype normalization* [3], and we call this best, alternative representation of a layout described by datatype t its *normalized form normal(t)*. The expectation is that an MPI library will indeed attempt to find a good normalized form at `MPI_Type_commit` time (if not, the user could do better by deriving the normalized form by himself and setting up the datatype in that way), which is formalized as the following

datatype normalization performance guideline:

$$\text{MPI_X}(c, t) \preceq \text{MPI_X}(c, \text{normal}(t)) \quad (\text{GL4})$$

That is, we expect the performance of a communication operation X with datatype t to be no worse than what can be achieved with the best, normalized description of the layout. The guideline is tricky, since the user may not readily be able to see what is the best way to describe a layout in a given situation. But in many cases he can give a good guess, and the guideline states that we would expect the `MPI_Type_commit` operation to do as well.

The normalization heuristics typically applied by MPI libraries replace more general type constructors (struct) with more specific ones (index or index block), collapse nested constructors, and identify large contiguous segments, where such replacements are applicable. Explicit descriptions of common type normalization heuristics can be found in [7, 8, 10, 12, 15]. As we will see in the following, there are natural layout descriptions that are *not* normalized by these heuristics, leading to severe violations of the guideline.

3.1 Communication Patterns

In our experiments, we will use the same three types of communication operations as in Section 2. In order to verify Guidelines (GL2) and (GL3), we extend the benchmarks with `MPI_Pack` and `MPI_Unpack` operations to achieve the same semantics as when datatype arguments were used directly in the communication calls:

1. Ping-pong (cf. Schneider *et al.* [14]): Ping side: `MPI_Pack` followed by `MPI_Send` followed by `MPI_Recv` followed by `MPI_Unpack`. Pong side: `MPI_Recv` followed by `MPI_Unpack` followed by `MPI_Pack` followed by `MPI_Send`.
2. Asymmetric (rooted) collective, e.g., `MPI_Bcast` on p processes. Root: `MPI_Pack` followed by `MPI_Bcast`. Non-roots: `MPI_Bcast` followed by `MPI_Unpack`.
3. Symmetric (non-rooted) collective, e.g., `MPI_Allgather` on p processes. All processes call `MPI_Pack`, followed by `MPI_Allgather`, then all processes perform p successive `MPI_Unpack` operations on the received, packed blocks.

In the `MPI_Allgather` pattern, the successive unpacking of the received blocks is necessary, since the catenation of packing units is not a packing unit [9, Section 4.2], so even if the received p packed blocks do form a contiguous piece of memory, it is not correct to unpack it with only one `MPI_Unpack` operation.

3.2 Experimental Results

The structure of experiments is guided by the guidelines, and we state for each experiment what our expectations (hypotheses) are, and comment on whether the results support or falsify them. As baseline we use in most cases the simple layouts of Section 2. We report results only for the `MPI_INT` basetype and the **Variant 1** basic layouts.

3.2.1 Expectation Test 3

For Guidelines (GL2) and (GL3), we first use the layouts of Section 2 with the same values for A and B and compare the benchmark performance with datatype communication against the performance with explicit pack and unpack operations.

Experiment.

Reference Layouts	Tiled (AB), Block ($A\bar{B}$) Bucket ($\bar{A}B$), Alternating ($\bar{A}\bar{B}$)
Compared Layouts	same layouts, but using <code>MPI_Pack</code> and <code>MPI_Unpack</code>
blocksize A	2, 10, 10 000
datasize m	64 000 Bytes to 2 560 000 Bytes
comm. patterns	Ping-pong, <code>MPI_Allgather</code> , <code>MPI_Bcast</code>
# of processes	32×1 , 1×16 (2×1 , 1×2 for Ping-pong)

Expectation.

We do not expect any MPI library to significantly violate the guidelines Guidelines (GL2) and (GL3), but with these simple layouts we hope to see cases where an MPI library performs significantly better with datatypes than with explicit packing and unpacking.

Results.

Much to our surprise, we found many cases where the guidelines are severely violated. For processes on different nodes, both the NEC MPI-1.3.1 and MVAPICH2-2.1 libraries violate the guidelines for all layouts, see Figure 4 for two examples. Especially with MVAPICH2-2.1, the violations are severe and amount to factors of two or more. With MPI processes on the same node, in many cases (with NEC MPI-1.3.1) MPI derived datatypes performed better than explicit packing and unpacking before and after communication. Examples with the `MPI_Bcast` pattern are shown in Figure 5.

3.2.2 Expectation Test 4

As a sanity check for Guideline (GL1), we create a contiguous n/k -element datatype with the `MPI_Type_contiguous` constructor for each of the k -element datatypes of Section 2. We compare the performance of the two datatypes against each other for different communication patterns.

Experiment.

Reference Layouts	Tiled (AB), Block ($A\bar{B}$) Bucket ($\bar{A}B$), Alternating ($\bar{A}\bar{B}$)
Compared Layouts	Contiguous-subtype with subtypes: Tiled (AB), Block ($A\bar{B}$) Bucket ($\bar{A}B$), Alternating ($\bar{A}\bar{B}$)
blocksize A	2, 10, 100, 1000, 1024, 10 000
datasize m	2000 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	2×1 , 1×2

Type description.

The concrete **Contiguous-subtype** is shown in Figure 6 with **Tiled (AB)** as subtype. The **Tiled (AB)** subtype consists of units of $k = A$ elements, and in the communication patterns, n/k such units are communicated. In contrast, the **Contiguous-subtype** contains all n/k units in a single type, so all n elements are communicated using a count of one with this datatype.

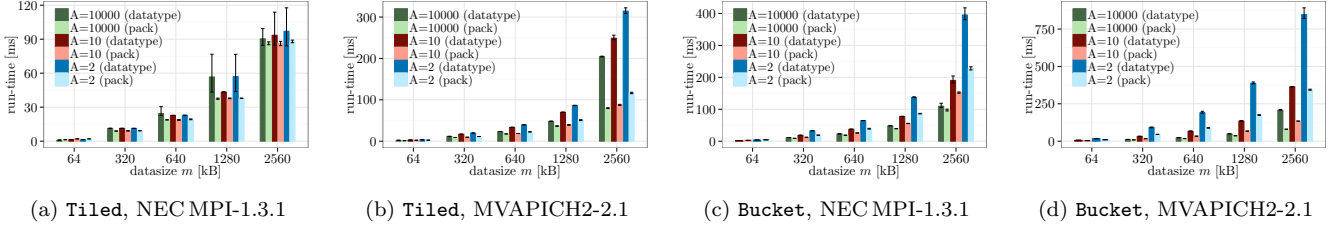


Figure 4: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, 32×1 processes, `MPI_Allgather`.

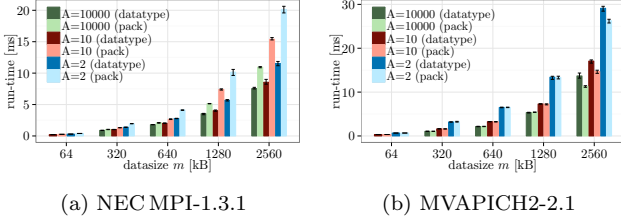


Figure 5: Alternating layout vs. pack/unpack, element datatype: `MPI_INT`, 1×16 processes, `MPI_Bcast`.

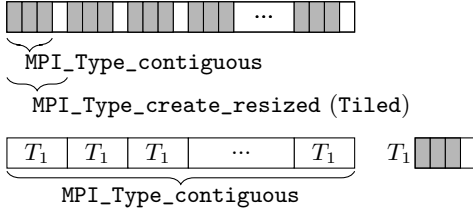


Figure 6: Basic, static layouts (in this figure `Tiled (AB)`, top) vs. `Contiguous-subtype` (bottom).

Expectation.

We expect no difference in performance between the reference and compared layouts.

Results.

Again, surprisingly, the MVAPICH2-2.1 (and also OpenMPI-1.10.1, not shown here) library violates the guideline for the `Tiled (AB)` type, with `Contiguous-subtype` being a factor of three slower with `Tiled (AB)` as subtype, see Figure 7. For the other basic types `Block (AB)`, `Bucket (AB)`, and `Alternating (AB)`, no significant performance difference between the left-hand and the right-hand side of Guideline (GL1) was detected.

3.2.3 Expectation Test 5

The remaining expectation tests are concerned with verifying Guideline (GL4). In all these tests, we give different descriptions of the same layout and study the communication performance. We formulate our expectations (hypotheses) on the assumption that a strong type normalization is not performed by the MPI libraries.

Our first experiment uses the regularly strided `Tiled (AB)` layout, for which we now know the baseline communication performance. We describe this pattern as a larger block comprised of several `Tiled (AB)` subtypes.

Experiment.

Reference Layout	Tiled (AB)
Compared Layout	Tiled-struct
blocksize A	2, 10, 100, 1000, 1024, 10 000
stride B	$A + 2$
repetition counts S_1, S_2	(a) $S_1 = 1, S_2 = 1$ (b) $S_1 = 2, S_2 = 3$
datsize m	2000 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	$2 \times 1, 1 \times 2$

Type description.

The `Tiled-struct` layout is a concatenation described with `MPI_Type_create_struct` of two smaller, contiguously strided layouts of S_1 and S_2 tiled blocks. The description is illustrated in Figure 8. Each `Tiled` sub-layout has the same blocksize A and stride B . The number of elements in the structure is $(S_1 + S_2)A$. We also allow the degenerated (fully contiguous) case of $A = B$. However, we only test the performance of the structured layout using $A < B$, with A and B chosen as in **Variant 1** (cf. Table 2).

Expectation.

As explained, since the user can easily describe the `Tiled` layout with the `MPI_Type_contiguous` and `MPI_Type_create_resized` constructor, we would like to expect that the MPI library can detect from the `Tiled-struct` description that the underlying pattern is a simple, tiled pattern. That would require detecting that both sub-layouts of the `MPI_Type_create_struct` are indeed tiled (although with different repetition counts) and have the same basetype. However, the heuristics used by MPI libraries at `MPI_Type_commit` time usually work differently [7, 8]. Therefore, we actually expect to see cases where the `Tiled-struct` description performs worse than the reference layout.

Results.

The results in Figure 9, especially for MVAPICH2-2.1, show a large performance difference for $A = 2$. Even in the case of $S_1 = S_2$, where the two subtypes are identically set up, the `Tiled-struct` performs several factors worse. This shows that the normalization heuristics in the MPI libraries are insufficient to identify the complex description of the simple, tiled layout and to normalize accordingly.

3.2.4 Expectation Test 6

The next experiment for Guideline (GL4) is also a sanity check, where we would expect no differences between two equally simple, natural descriptions of a tiled layout. We now describe the `Tiled (AB)` layout as a vector of n/A contiguous blocks of A elements with stride B . This is the “most

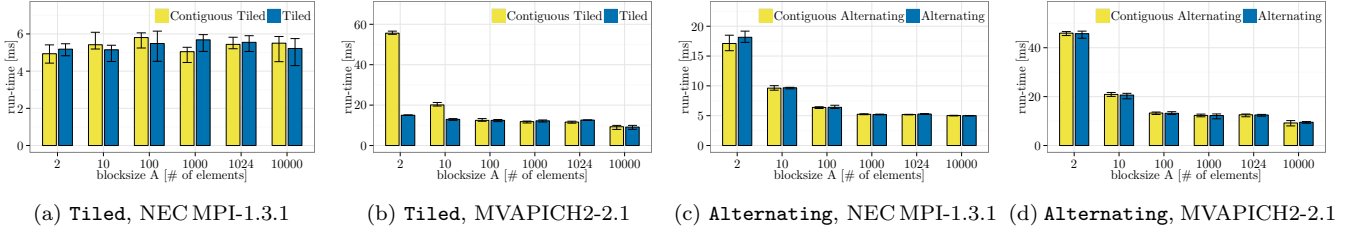


Figure 7: Basic layouts vs. **Contiguous-subtype**, $m = 2.56$ MBytes, element datatype: **MPI_INT**, 2×1 processes, Ping-pong.

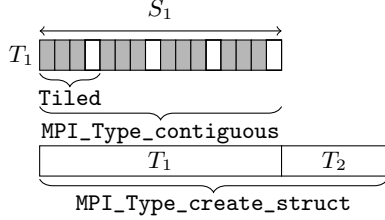


Figure 8: **Tiled** (top) vs. **Tiled-struct** (bottom).

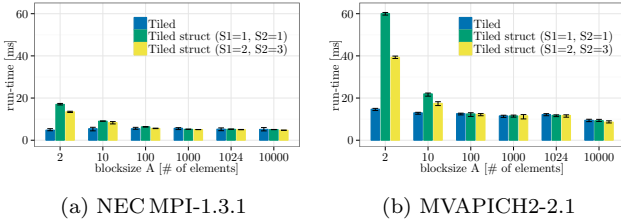


Figure 9: **Tiled (AB)** vs. **Tiled-struct**, element datatype: **MPI_INT**, $m = 2.56$ MBytes, 2 nodes, Ping-pong.

natural” way in MPI to describe a long, regularly strided layout, and is accomplished with **MPI_Type_vector**. To have the same extent of the vector type, we resize the extent of the vector to n/A times the extent of **Tiled (AB)**. The **Tiled-vector** datatype is our first example of a *dynamically derived datatype* that can only be set up when the number of elements n to be communicated is known. As in all our experiments, we do *not* include the datatype setup time in the measured run-time.

Experiment.

Reference Layout	Tiled (AB)
Compared Layout	Tiled-vector
blocksize A	2, 10, 100, 1000, 1024, 10000
stride B	$A + 2$
datasize m	2000 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	2×1 , 1×2

Type description.

The two contrasted datatype layout descriptions **Tiled (AB)** and **Tiled-vector** are illustrated in Figure 10.

Expectation.

We expect the performance of the two descriptions to match. The MPI internal representations of the two descriptions can be expected to be similar, and concrete offsets for accessing the elements in the layout can be computed easily

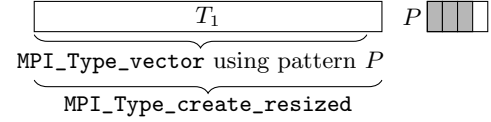


Figure 10: **Tiled-vector** defines the layout with **MPI_Type_vector** using the **Tiled** pattern.

by the datatype engine given these representations. Since the **MPI_Type_vector** is a commonly used datatype constructor, it may even have been specially optimized, such that the description as **Tiled-vector** might be slightly advantageous.

Results.

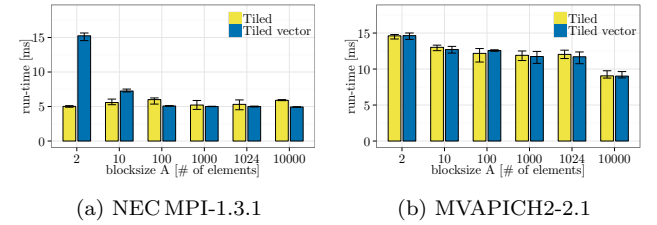


Figure 11: **Tiled (AB)** vs. **Tiled-vector**, element datatype: **MPI_INT**, $m = 2.56$ MBytes, 2 nodes, Ping-pong.

As shown in Figure 11, for the NEC MPI-1.3.1 (and also for OpenMPI-1.10.1) library and small values of A , the **Tiled-vector** performs much worse than repeating the **Tiled (AB)** block. This is again surprising. However, the comparison of the absolute performance between NEC MPI-1.3.1 and MVAPICH2-2.1 shows that the bad performance of **Tiled-vector** is relative, in absolute terms it is on par with the performance in MVAPICH2-2.1 for both descriptions of the layout. These findings also illustrate that performance guidelines can only ensure consistency in an MPI library. Guideline verification needs to be complemented with benchmarking against hard baselines.

3.2.5 Expectation Test 7

Our next description of the **Tiled (AB)** layout is done using a nested vector. We describe a larger block of a constant S number of units of A elements and stride B with the **MPI_Type_vector** constructor. On this datatype, we build a dynamic vector of $n/(SA)$ blocks with a stride of SB elements. In order to express the stride correctly, this vector has to be constructed with the **MPI_Type_hvector** constructor.

Experiment.

Reference Layout	Tiled (AB)
Compared Layout	Vector-tiled
blocksize A	2, 10, 100, 1000, 1024, 10 000
stride B	$A + 2$
datsize m	2000 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	$2 \times 1, 1 \times 2$

Type description.

The setup of the nested vector **Vector-tiled** versus the basic layout **Tiled (AB)** is illustrated in Figure 12.

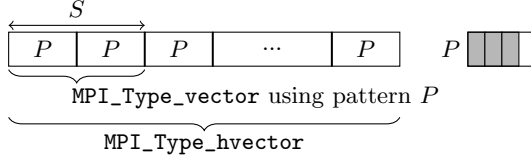


Figure 12: Vector-tiled

Expectation.

We expect that an MPI library will detect that the stride for the outer vector is equal to c times the stride of the inner vector, such that the layout can also be described by a non-nested vector constructor. **MPI_Type_commit** should perform the transformation. The performance of the two descriptions should therefore be similar, regardless of the communication pattern.

Results.

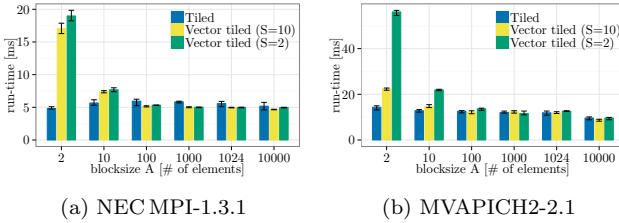


Figure 13: **Tiled (AB)** vs. **Vector-tiled**, element datatype: **MPI_INT**, $m = 2.56$ MBytes, 2 nodes, Ping-pong.

To our surprise, apparently none of the MPI libraries normalizes the two-level nested vector description into a better layout. For a small unit of size $A = 2$, the communication time with **Vector-tiled** compared to the communication time with the simple **Tiled (AB)** description differ by factors from 2 to 4, as shown in Figure 13.

3.2.6 Expectation Test 8

In this experiment, we look at different, explicit descriptions of the more irregular layout **Block ($A\bar{B}$)**, by explicitly listing the displacements and number of elements in all n/k blocks in the n element layouts. The purpose of this experiment is to investigate the relative penalty of having to traverse long, explicit lists of displacements, versus implicit, computed displacements.

Experiment.

Reference Layout	Block ($A\bar{B}$)
Compared Layout	Block-indexed
blocksize A	2, 10, 100, 1000, 1024, 10 000
stride B	$B_1 = A + 1, B_2 = A + 3$
datsize m	3200 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	$2 \times 1, 1 \times 2$

Type description.

The **Block-indexed** layout uses the **Block** layout with given A, B_1 , and B_2 , described with the **MPI_Type_create_indexed_block** constructor with n/A indices and blocksize A . The block displacements can easily be computed. This is illustrated in Figure 14.

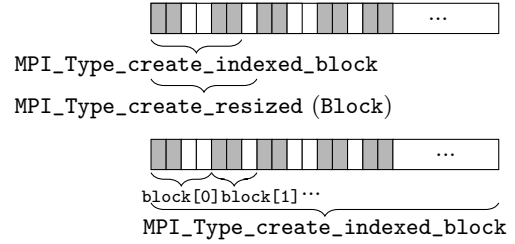


Figure 14: Static **Block ($A\bar{B}$)** (top) vs. dynamic **Block-indexed** (bottom) description of the **Block ($A\bar{B}$)** layout.

Expectation.

An MPI library should normalize both cases to the same internal datatype representation with good performance. It is doubtful that anything like that will happen. More importantly, it is not obvious which of the two descriptions is better. A reasonable expectation is that beyond some number of elements, the large array of displacements (indices) in the **Block-indexed** datatype will become expensive to traverse, and that simple repetitions of the small, irregular non-contiguous **Block** pattern will perform better.

Results.

For small blocksizes of A , the **Block** description is worse, especially for the NEC MPI-1.3.1 library. Otherwise the performance of the two descriptions looks similar. Nevertheless, the absolute performance of the NEC MPI-1.3.1 library is still better. We do not show the results here (see appendix).

3.2.7 Expectation Test 9

This experiment is similar to the previous one. Here, two descriptions of the “most irregular” of the four basic layouts, namely **Alternating ($A\bar{B}$)** are contrasted.

Experiment.

Reference Layout	Alternating ($A\bar{B}$)
Compared Layout	Alternating-indexed
blocksize A	2, 10, 100, 1000, 1024, 10 000
blocksize A_1, A_2	$A_1 = A - 1, A_2 = A + 1$
stride B	$B_1 = A + 1, B_2 = A + 3$
datsize m	3200 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	$2 \times 1, 1 \times 2$

Type description.

The **Alternating-indexed** datatype is based on the **Alternating** layout with given A_1, A_2, B_1 , and B_2 , described with the **MPI_Type_indexed** constructor with $n/(A_1 + A_2)$ indices and blocksizes of A_1 and A_2 . The data layout is illustrated in Figure 15.



Figure 15: Static **Alternating** ($\bar{A}\bar{B}$) (top) vs. dynamic **Alternating-indexed** (bottom) description of the **Alternating** ($\bar{A}\bar{B}$) layout.

Expectation.

As for the previous experiment, it is not obvious which of the two descriptions will perform better (under the pessimistic assumption that no normalization takes place). Experimental results will give insight on whether there is a penalty for large lists of displacements in the **MPI_Type_indexed** constructor.

Results.

For larger values of A , the performance of the two descriptions looks similar. For small values of A , the results are the opposite of the previous experiment. Especially for the NEC MPI-1.3.1, the **Alternating-indexed** description performs worse than the **Alternating** ($\bar{A}\bar{B}$) description. Results are not shown here (see appendix).

3.2.8 Expectation Test 10

In our final test with the basic layouts, we look at an **Alternating** ($\bar{A}\bar{B}$) pattern where the stride B_2 of the second unit is equal to the number of elements A_2 in the unit. This pattern can be described as a repetition of small datatypes describing fixed blocks. It can alternatively be formulated as a layout comprised of (1) a first, small unit of A_1 elements, (2) a large, regularly strided middle part, and (3) a last, small unit of A_2 elements. We expect the second description to perform better, and we want to check this hypothesis.

Experiment.

Compared Layouts	Alternating-repeated Alternating-struct
blocksize A	2, 10, 100, 1000, 1024, 10000
unit blocksizes A_1, A_2	$A_1 = A - 1, A_2 = A + 1$
stride B	$A + 1$
datasize m	3200 Bytes, 2 560 000 Bytes
comm. patterns	Ping-pong
# of processes	$2 \times 1, 1 \times 2$

Type description.

Here, two types describe an **alternating** layout with units

of A_1 and A_2 elements and strides $B_1 = B$ and $B_2 = A_2$, respectively. The first datatype is called **Alternating-repeated** and is defined as a fixed, alternating block (Figure 16a). The second is called **Alternating-struct** and is created with **MPI_Type_create_struct** using three subtypes: the first is a block of A_1 contiguous elements, the second subtype is a tiled vector, and the third subtype is a contiguous block of A_2 elements (Figure 16b).

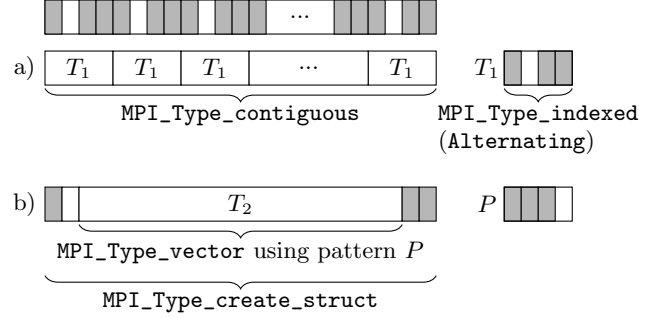


Figure 16: **Alternating-repeated** (top) vs. **Alternating-struct** (bottom).

Expectation.

With the description as an **Alternating-struct**, communication performance should approach the performance of communicating a tiled vector with blocksizes of $A_1 + A_2$ elements, when the total number of elements n goes up. Our previous measurements have given the baseline performance for such **Tiled** (AB) patterns, against which we can compare. Since commonly used MPI normalization heuristics do probably not change the description from **Alternating-repeated** to the possibly better **Alternating-struct**, our expectation is that the latter will perform better.

Results.

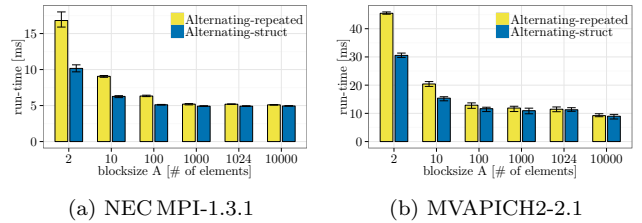


Figure 17: **Alternating-repeated** vs. **Alternating-struct**, element datatype: **MPI_INT**, $m = 2.56$ MBytes, 2 nodes, Ping-pong.

For small values of A , the **Alternating-repeated** way of communicating the pattern is indeed slower for all tested MPI libraries; see Figure 17. This shows that a stronger type normalization (on the fly) than currently performed by MPI libraries is needed to approach the baseline performance. It also shows, and this is important, that the **MPI_Type_create_struct** constructor is needed for the best description even of homogeneous layouts where all elements have the same basic type.

3.2.9 Expectation Test 11

For our final set of experiments, we use another layout. Given an $(n + 1 - A) \times A$ matrix, we want to communicate together the first row of A elements and the (remainder of the) first column of $n - A$ elements, for a total of n elements. For examining Guideline (GL4), we again compare natural ways of describing this layout, and compare the measured communication times. A similar example was used by Galian *et al.* [2].

Experiment.

Compared Layouts	RowCol-fully-indexed RowCol-contiguous-and-indexed RowCol-struct
blocksize A	2, 10, 100, 128, 512, 1000, 1024, 5000, 10 000
# of elements n	100, 10 240
comm. patterns	Ping-pong
# of processes	2×1 , 1×2

Type description.

A row-column layout (submatrix of $(n + 1 - A) \times A$ matrix), consisting of A consecutive elements followed by $n - A$ elements in a strided layout with stride A , can be described either by

1. using `MPI_Type_create_indexed_block` with n indices (RowCol-fully-indexed),
2. using `MPI_Type_indexed` with $1 + n - A$ indices (RowCol-contiguous-and-indexed), or
3. using `MPI_Type_create_struct` consisting of a contiguous subtype of A elements, followed by a vector of $n - A$ blocks of one element with stride A (RowCol-struct).

The layout and the three possible descriptions as derived datatypes are shown in Figure 18.

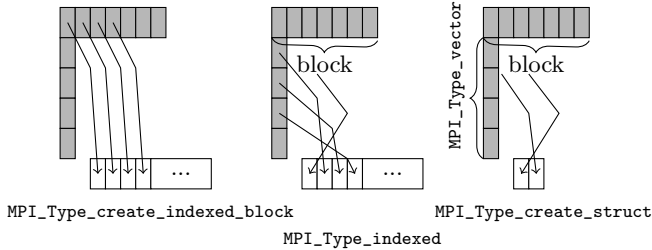


Figure 18: From left to right: RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct.

Expectation.

The latter representation is the most compact, and expectedly best performing. This layout description also illustrates that the full power of the `MPI_Type_create_struct` constructor is needed, even for homogeneous layouts of elements of the same basic type. As we do not expect the MPI libraries to perform a normalization into an efficient data representation, our hypothesis is that the RowCol-struct datatype will perform better than the two other types, and that RowCol-contiguous-and-indexed may perform better than RowCol-fully-indexed as the blocksize A goes up.

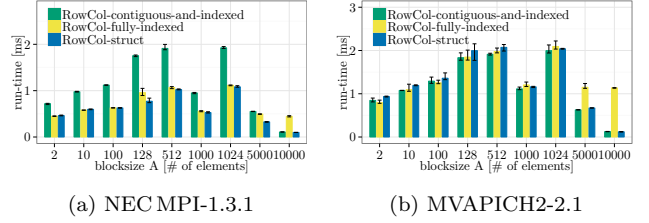


Figure 19: RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct, element datatype: MPI_INT, $n = 10\,240$, extent increases with A , 2 nodes, Ping-pong.

Results.

The results in Figure 19 confirm that for NEC MPI-1.3.1 the compact description RowCol-struct gives the best performance, closely followed by RowCol-fully-indexed. For the MVAPICH2-2.1, the performance is worse (compared to NEC MPI-1.3.1 as baseline) for all three descriptions, except for large values of A . The results for OpenMPI-1.10.1 (see appendix) are as expected, with the compact RowCol-struct description being close to a factor of two faster than the other two (except for the large A values).

4. SUMMARY AND OUTLOOK

We performed a large number of experiments to explore the performance of communication with differently structured, non-contiguous data layouts described by MPI derived datatypes. We focused on simple tiled layouts parameterized by element counts and strides, and structured the experiments as a set of expectation tests using MPI performance guidelines.

The results were revealing and in many cases surprising and disappointing. For instance, it was unexpected that Guidelines (GL2) and (GL3) would be violated, but we found many cases (for all libraries) where these guidelines were severely compromised. In such cases, the recommendation to use datatypes is hard to justify. It is definitely important to look into the reasons and improve the situation. We also observe that the communication performance with (non-trivial) derived datatypes is quite different between the libraries. For example, the current version of MVAPICH does not handle derived datatypes as efficiently as the other libraries.

In addition, the simplest expectations concerning the use of the `MPI_Type_contiguous` constructor, captured in Guideline (GL1), were sometimes violated. We believe that these violations can and should be repaired.

Our experiments around Guideline (GL4) first and foremost show that the way a given layout is described as a derived datatype matters a lot. Or put differently, the heuristics employed by common MPI libraries in `MPI_Type_commit` are insufficient to find good internal datatype representations. It is worthwhile to improve the situation, since an application programmer currently needs a good intuition to select an efficient derived datatype description. Simple rules of thumb are not enough: our findings sometimes contradicted our own intuitions and expectations. Furthermore, some experiments show that datatype descriptions may be too localized to make a sufficiently good normalization possible, namely, that both the repetition count and the datatype are needed for computing the normalized type descrip-

tion. However, normalization on the fly in each communication call is not an option for a high-performance MPI library, especially since (optimal) normalization may be very expensive [2]. Therefore, the performance equivalence of the seemingly innocent Guideline (GL1) cannot hold when `MPI_Type_commit` may normalize the contiguous type (right-hand side of the guideline). MPI might need more query functionality for the application programmer to explore and guide the normalization.

5. ACKNOWLEDGMENTS

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APPENDIX

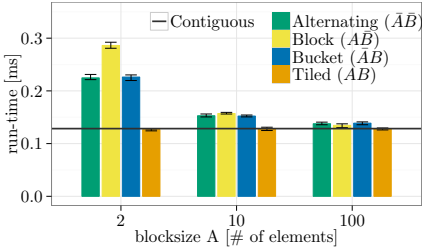
This appendix contains our currently full set of experiments, only some of which are shown in the main text. The results are listed in the order of the expectation tests.

A. EXPERIMENTAL RESULTS

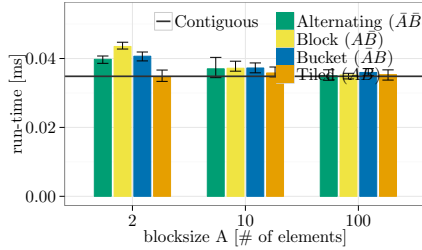
A.1 Expectation Test 1 (Sect. 2.4.1)

- Contiguous, Tiled (AB), Block ($A\bar{B}$), Bucket ($\bar{A}B$), Alternating ($\bar{A}\bar{B}$)
- Ping-pong, MPI_Bcast, MPI_Allgather

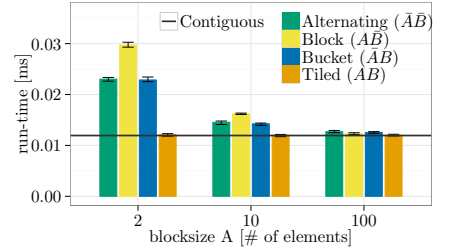
- Figure 20: NEC MPI-1.3.1, small datasize, **Variant 1**
- Figure 21: MVAPICH2-2.1, small datasize, **Variant 1**
- Figure 22: OpenMPI-1.10.1, small datasize, **Variant 1**
- Figure 23: NEC MPI-1.3.1, large datasize, **Variant 1**
- Figure 24: MVAPICH2-2.1, large datasize, **Variant 1**
- Figure 25: OpenMPI-1.10.1, large datasize, **Variant 1**, one node
- Figure 26: NEC MPI-1.3.1, small datasize, **Variant 1**, one node
- Figure 27: MVAPICH2-2.1, small datasize, **Variant 1**, one node
- Figure 28: OpenMPI-1.10.1, small datasize, **Variant 1**, one node
- Figure 29: NEC MPI-1.3.1, large datasize, **Variant 1**, one node
- Figure 30: MVAPICH2-2.1, large datasize, **Variant 1**, one node
- Figure 31: OpenMPI-1.10.1, large datasize, **Variant 1**, one node
- Figure 32: MVAPICH2-2.1, small datasize, **Variant 2**
- Figure 33: MVAPICH2-2.1, large datasize, **Variant 2**
- Figure 34: MVAPICH2-2.1, small datasize, **Variant 2**, one node
- Figure 35: MVAPICH2-2.1, large datasize, **Variant 2**, one node



(a) MPI_Allgather

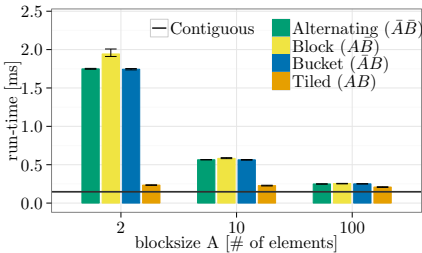


(b) MPI_Bcast

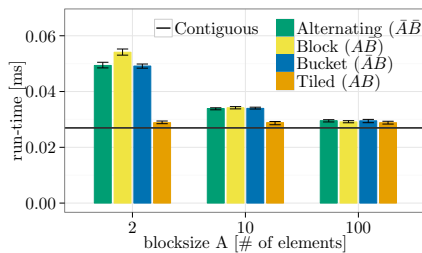


(c) Ping-pong

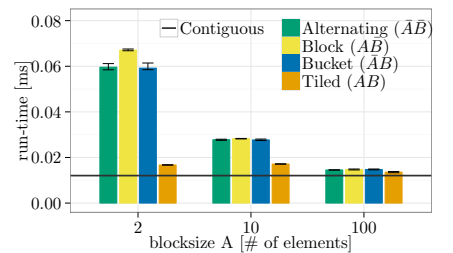
Figure 20: Contiguous vs. typed, $m = 3.2kBytes$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), NEC MPI-1.3.1, **Variant 1**.



(a) MPI_Allgather



(b) MPI_Bcast



(c) Ping-pong

Figure 21: Contiguous vs. typed, $m = 3.2kBytes$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), MVAPICH2-2.1, **Variant 1**.

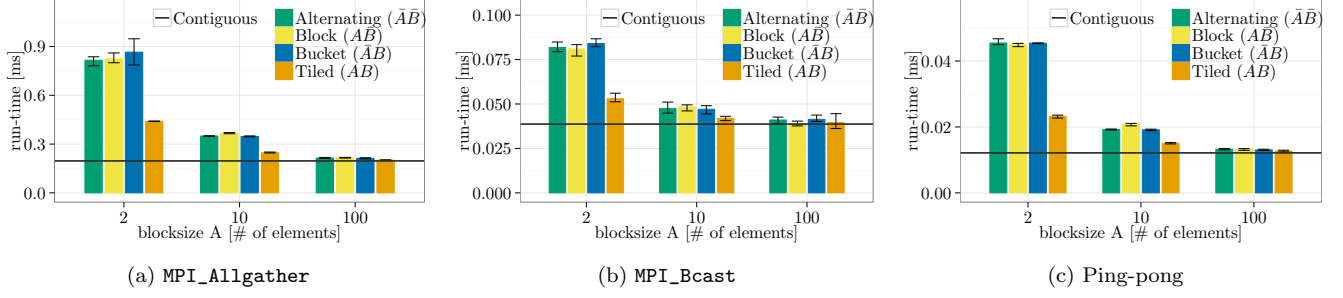


Figure 22: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), OpenMPI-1.10.1, **Variant 1**.

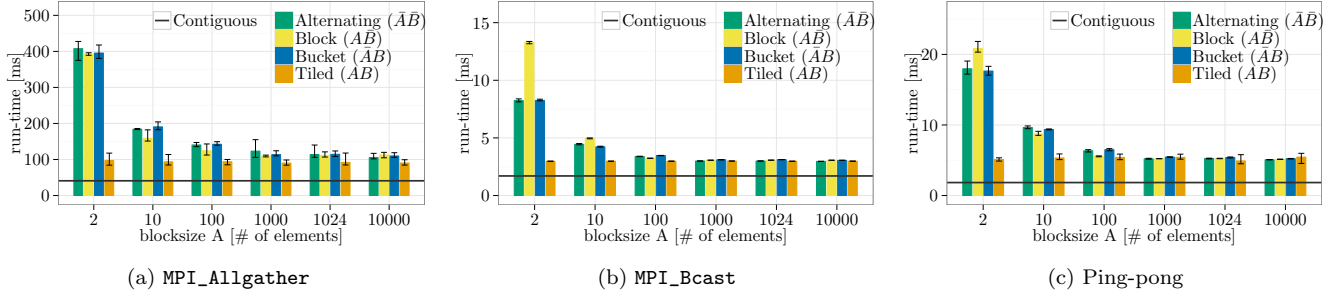


Figure 23: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), NECMPI-1.3.1, **Variant 1**.

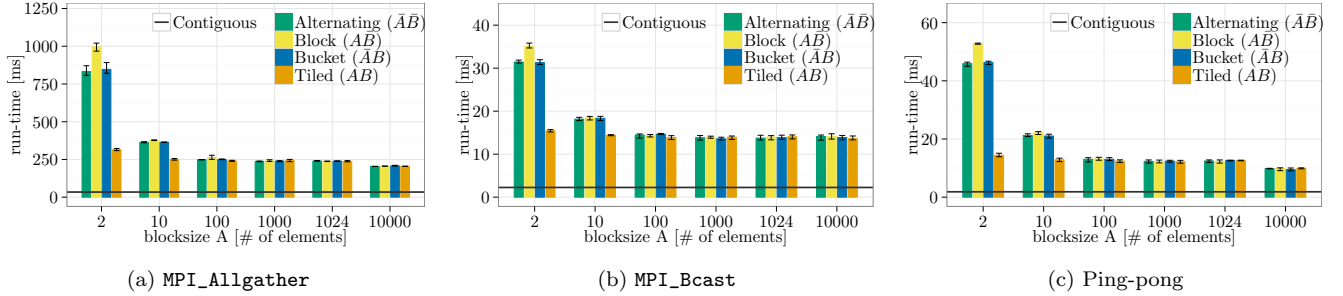


Figure 24: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), MVAPICH2-2.1, **Variant 1**.

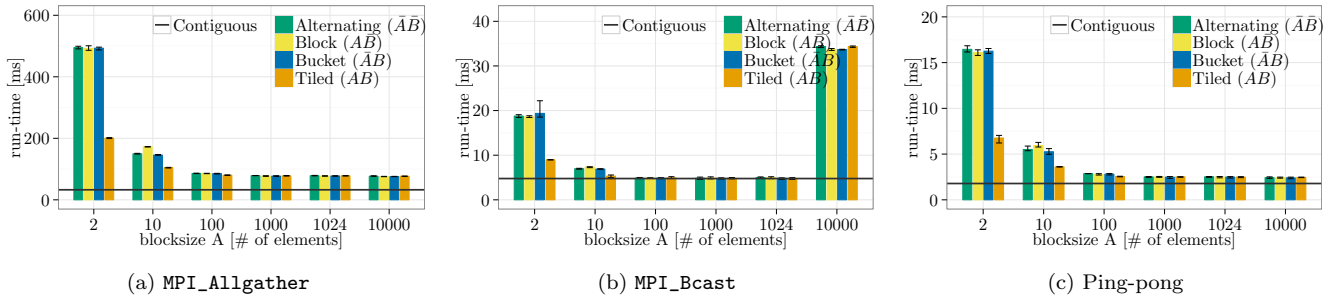


Figure 25: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), OpenMPI-1.10.1, **Variant 1**.

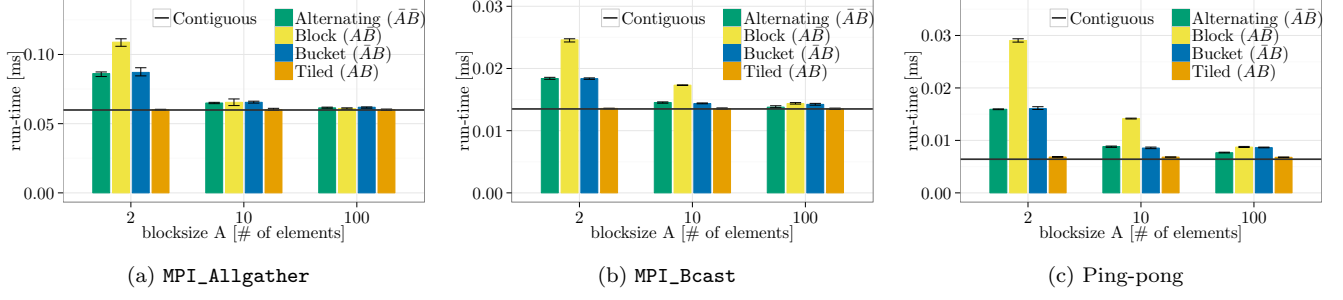


Figure 26: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, one node, 16 processes (2 for Ping-pong), NEC MPI-1.3.1, **Variant 1**.

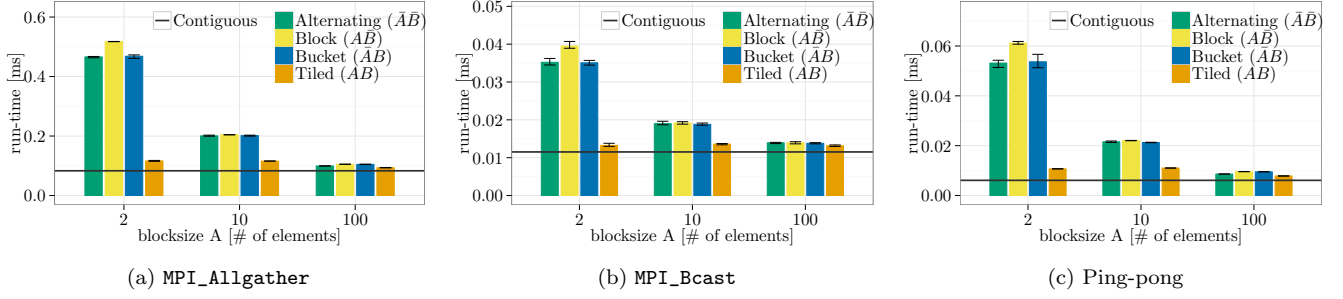


Figure 27: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, one node, 16 processes (2 processes for Ping-pong), MVAPICH2-2.1, **Variant 1**.

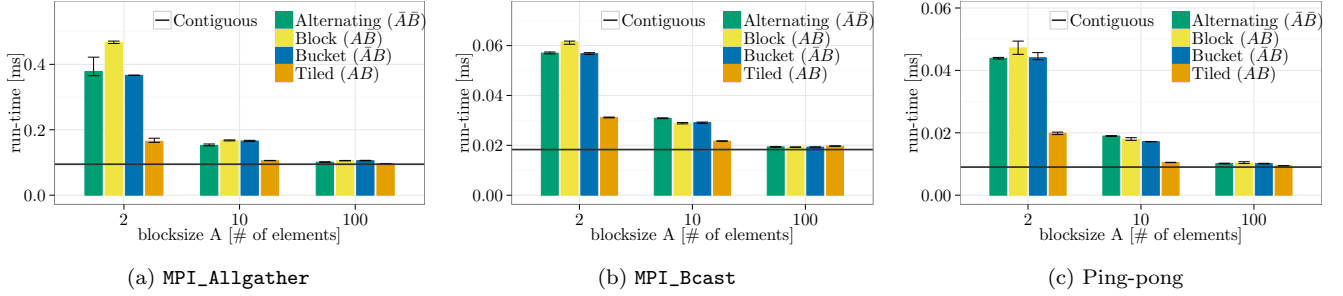


Figure 28: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, 1 node, 16 processes (2 processes for Ping-pong), OpenMPI-1.10.1, **Variant 1**.

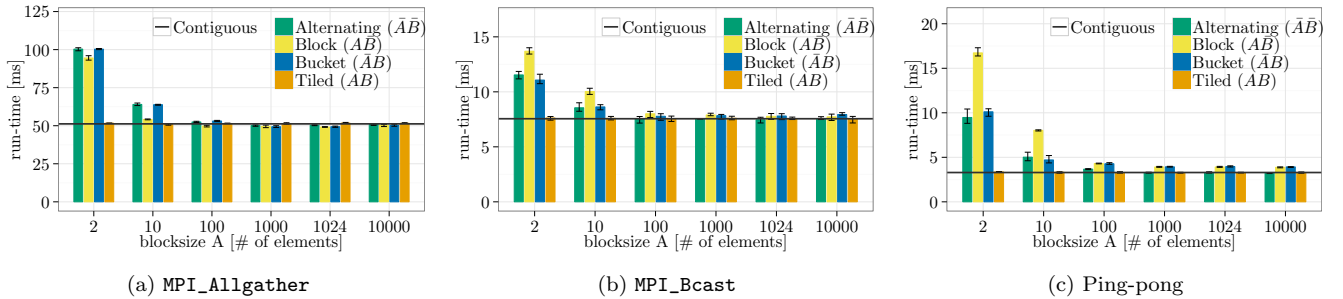


Figure 29: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, one node, 16 processes (2 processes for Ping-pong), NEC MPI-1.3.1, **Variant 1**.

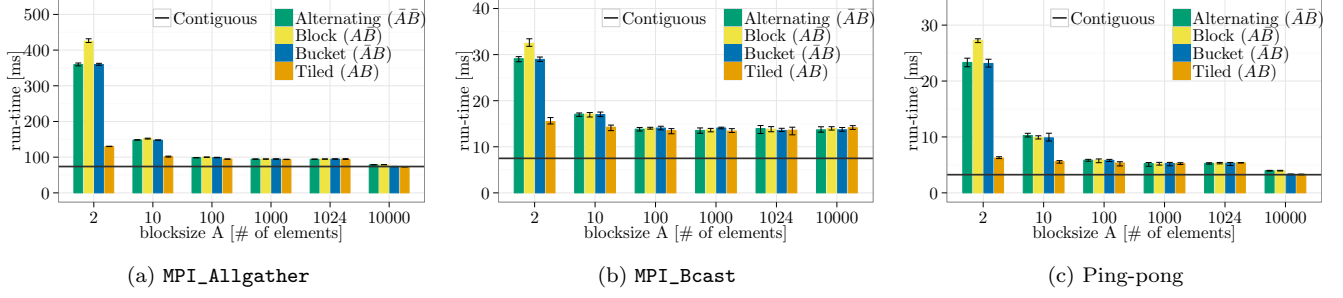


Figure 30: Contiguous vs. typed, $m = 2.56$ MBytes, element datatype: MPI_INT, one node, 16 processes (2 processes for Ping-pong), MVAPICH2-2.1, **Variant 1**.

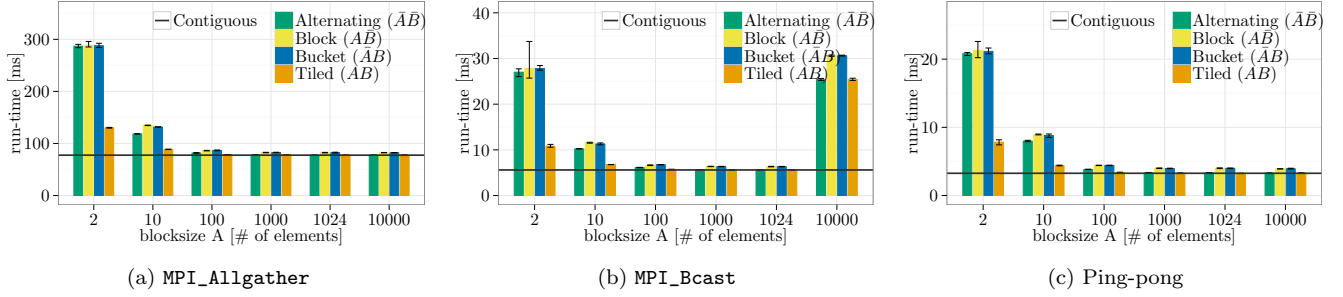


Figure 31: Contiguous vs. typed, $m = 2.56$ MBytes, element datatype: MPI_INT, 1 node, 16 processes (2 processes for Ping-pong), OpenMPI-1.10.1, **Variant 1**.

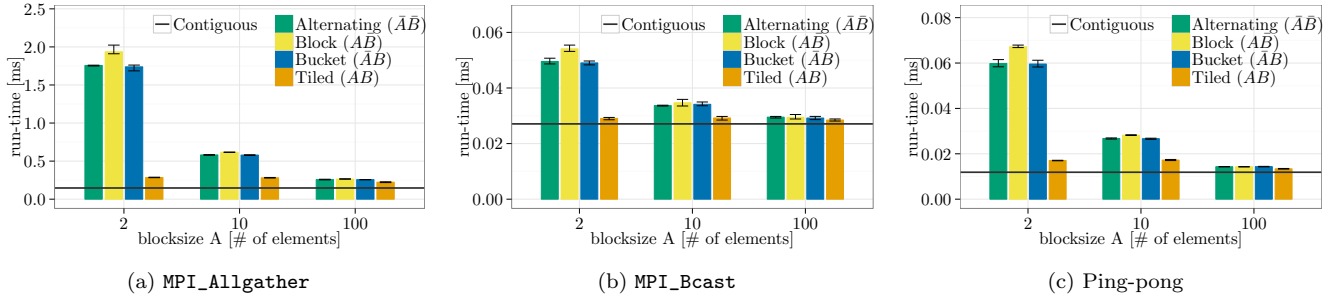


Figure 32: Contiguous vs. typed, $m = 3.2$ kBytes, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), MVAPICH2-2.1, **Variant 2**.

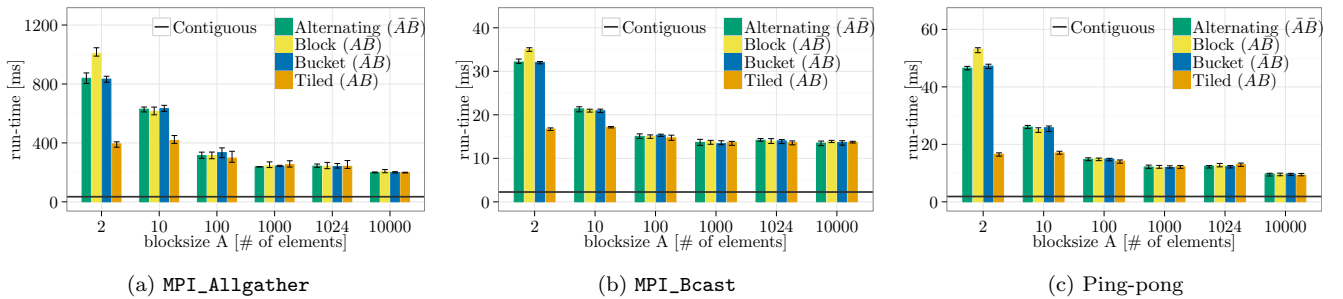


Figure 33: Contiguous vs. typed, $m = 2.56$ MBytes, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), MVAPICH2-2.1, **Variant 2**.

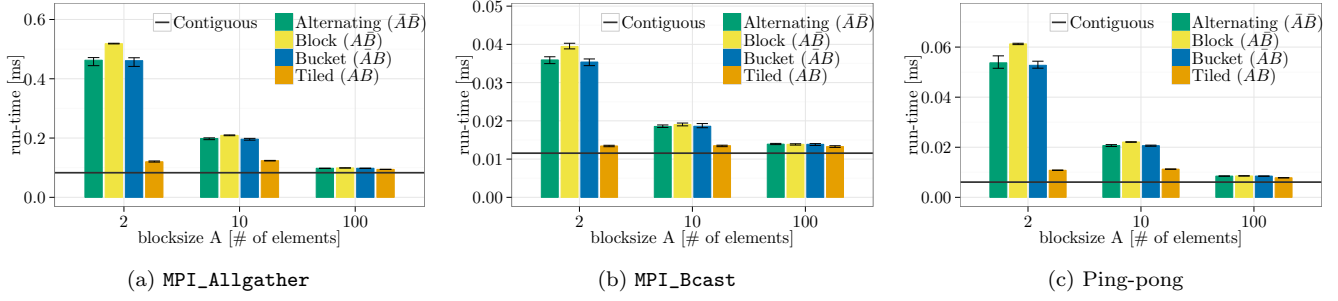


Figure 34: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, one node, 16 processes (2 for Ping-pong), MVAPICH2-2.1, **Variant 2**.

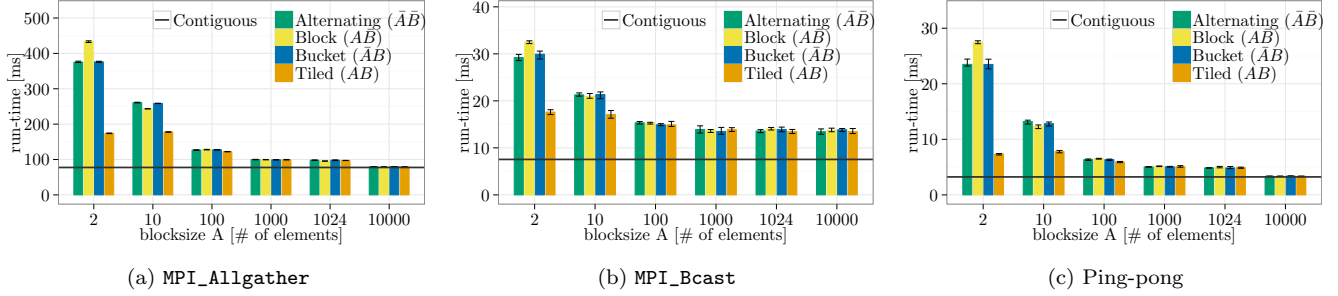


Figure 35: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, one node, 16 processes (2 for Ping-pong), MVAPICH2-2.1, **Variant 2**.

A.2 Expectation Test 2 (Sect. 2.4.2)

- Contiguous, Tiled-heterogeneous ($\bar{A}\bar{B}\bar{T}$)
 - Ping-pong
-
- Figure 36: NEC MPI-1.3.1
 - Figure 37: MVAPICH2-2.1
 - Figure 38: OpenMPI-1.10.1
-

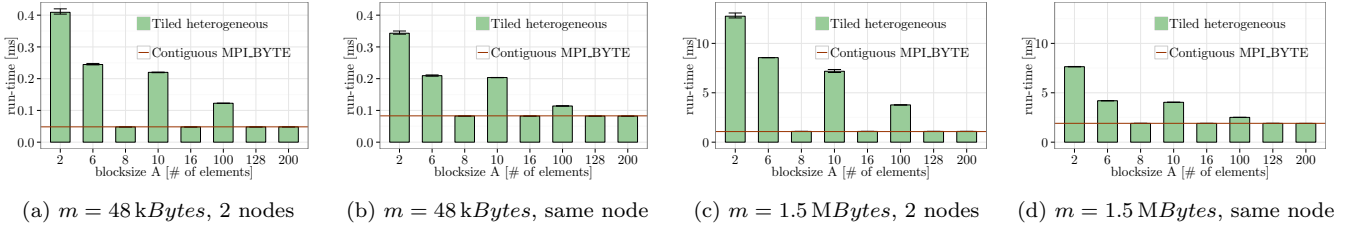


Figure 36: Contiguous vs. Tiled-heterogeneous ($\bar{A}\bar{B}\bar{T}$) $A=B$, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.

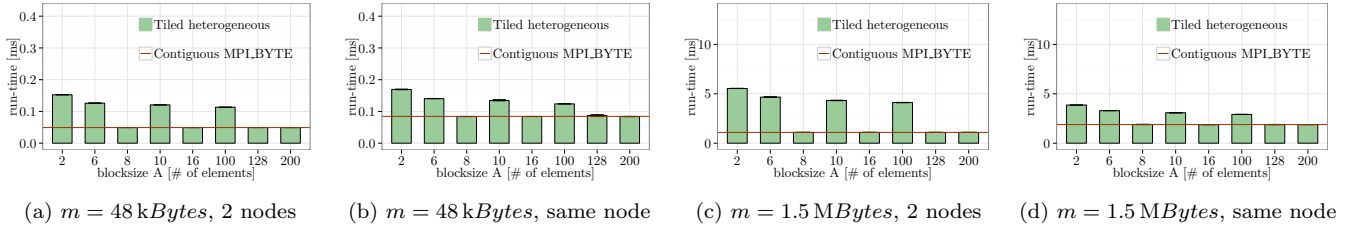


Figure 37: Contiguous vs. Tiled-heterogeneous ($AB\bar{T}$) $A=B$, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.

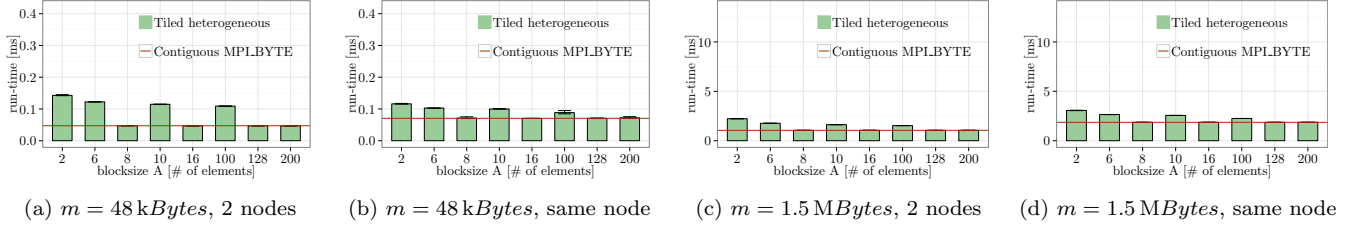


Figure 38: Contiguous vs. Tiled-heterogeneous ($AB\bar{T}$) $A=B$, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

A.3 Expectation Test 3 (Sect. 3.2.1)

- pack vs. unpack for basic layouts (Tiled, Block, Bucket, Alternating)
- MPI_Allgather, MPI_Bcast, Ping-pong
- Figure 39: NEC MPI-1.3.1, Ping-pong, 2×1 processes
- Figure 40: MVAPICH2-2.1, Ping-pong, 2×1 processes
- Figure 41: OpenMPI-1.10.1, Ping-pong, 2×1 processes
- Figure 42: NEC MPI-1.3.1, MPI_Allgather, 32×1 processes
- Figure 43: MVAPICH2-2.1, MPI_Allgather, 32×1 processes
- Figure 44: OpenMPI-1.10.1, MPI_Allgather, 32×1 processes
- Figure 45: NEC MPI-1.3.1, MPI_Bcast, 32×1 processes
- Figure 46: MVAPICH2-2.1, MPI_Bcast, 32×1 processes
- Figure 47: OpenMPI-1.10.1, MPI_Bcast, 32×1 processes
- Figure 48: NEC MPI-1.3.1, Ping-pong, one node, 2 processes
- Figure 49: MVAPICH2-2.1, Ping-pong, one node, 2 processes
- Figure 50: OpenMPI-1.10.1, Ping-pong, one node, 2 processes
- Figure 51: NEC MPI-1.3.1, MPI_Allgather, one node, 16 processes
- Figure 52: MVAPICH2-2.1, MPI_Allgather, one node, 16 processes
- Figure 53: OpenMPI-1.10.1, MPI_Allgather, one node, 16 processes
- Figure 54: NEC MPI-1.3.1, MPI_Bcast, one node, 16 processes
- Figure 55: MVAPICH2-2.1, MPI_Bcast, one node, 16 processes
- Figure 56: OpenMPI-1.10.1, MPI_Bcast, one node, 16 processes

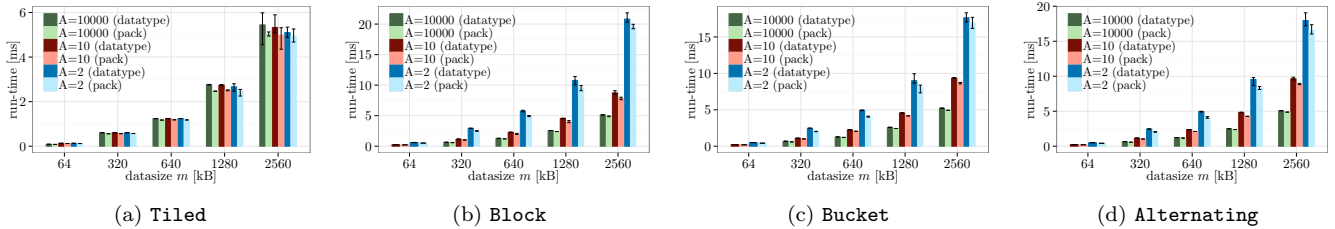


Figure 39: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 2×1 processes, Ping-pong, NEC MPI-1.3.1.

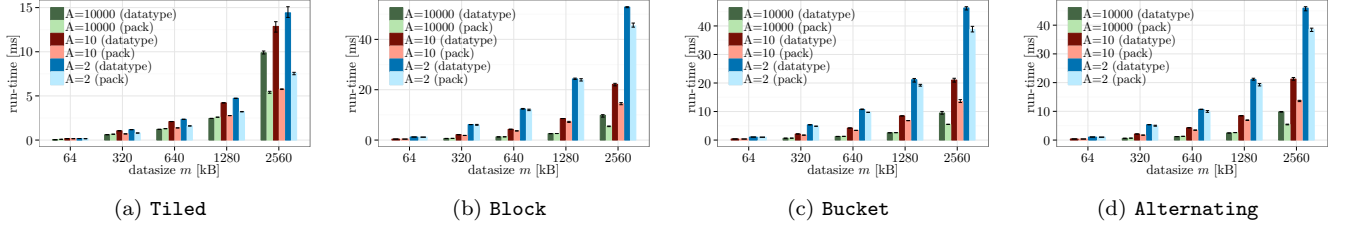


Figure 40: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 2×1 processes, Ping-pong, MVAPICH2-2.1.

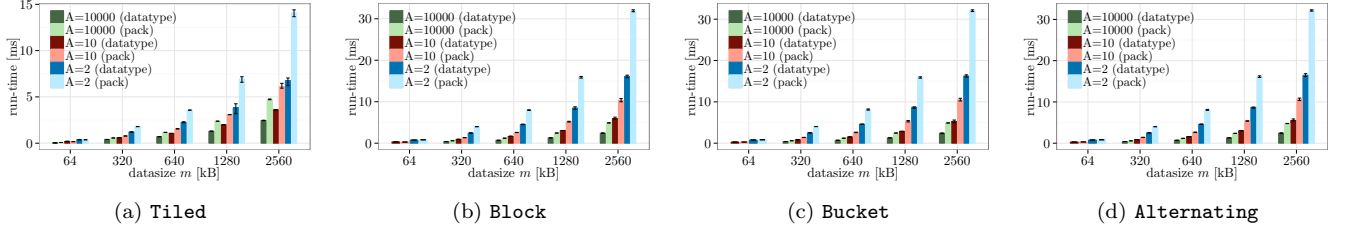


Figure 41: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 2×1 processes, Ping-pong, OpenMPI-1.10.1.

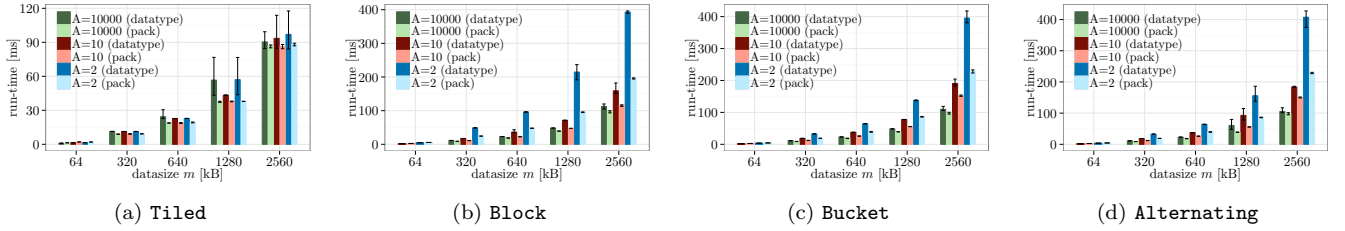


Figure 42: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 32×1 processes, MPI_Allgather, NEC MPI-1.3.1.

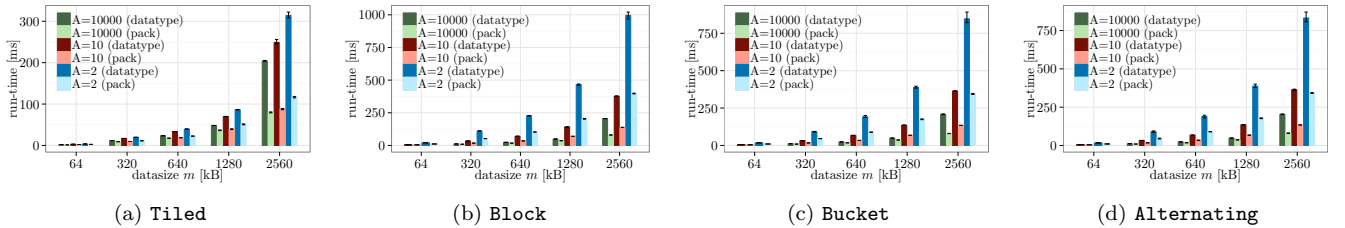


Figure 43: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 32×1 processes, MPI_Allgather, MVAPICH2-2.1.

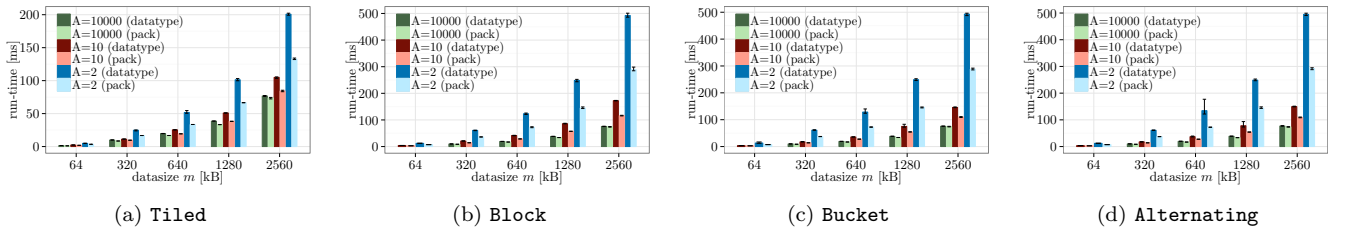


Figure 44: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 32×1 processes, MPI_Allgather, OpenMPI-1.10.1.

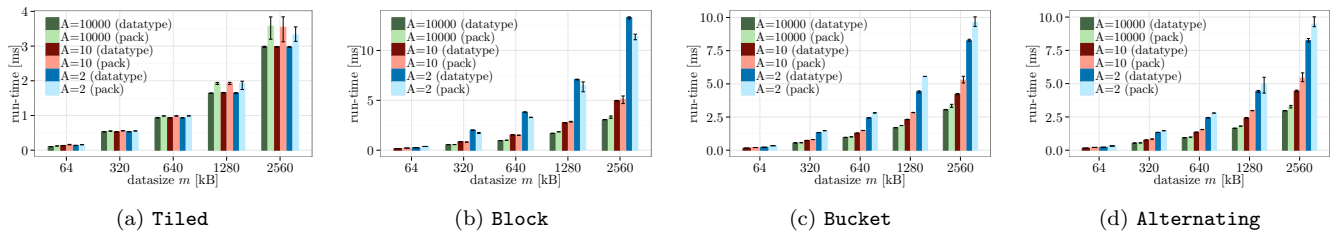


Figure 45: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, 32×1 processes, `MPI_Bcast`, NEC MPI-1.3.1.

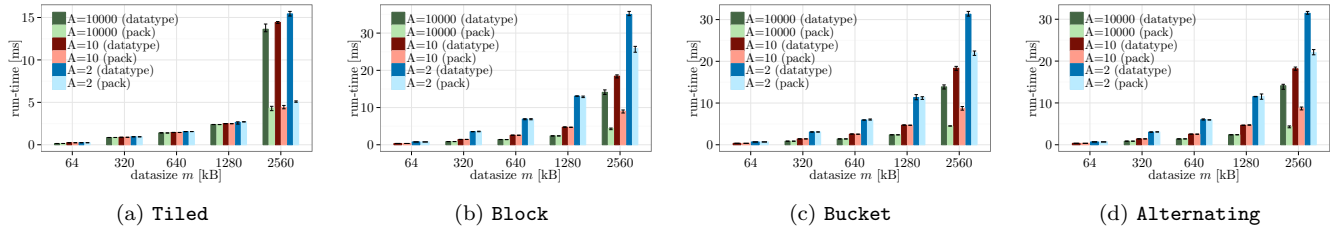


Figure 46: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, 32×1 processes, `MPI_Bcast`, MVAPICH2-2.1.

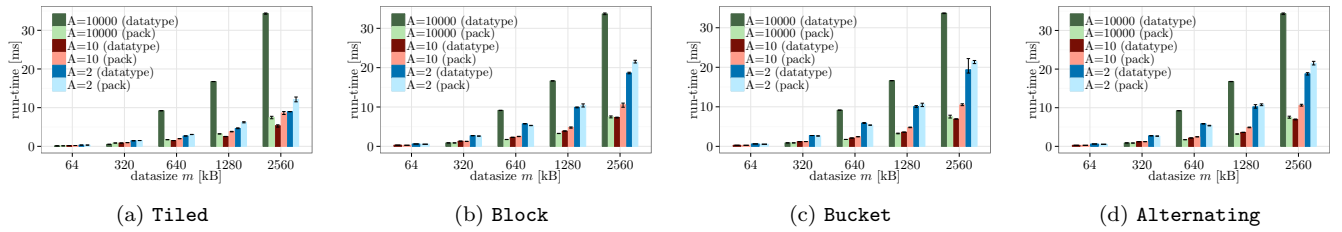


Figure 47: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, 32×1 processes, `MPI_Bcast`, OpenMPI-1.10.1.

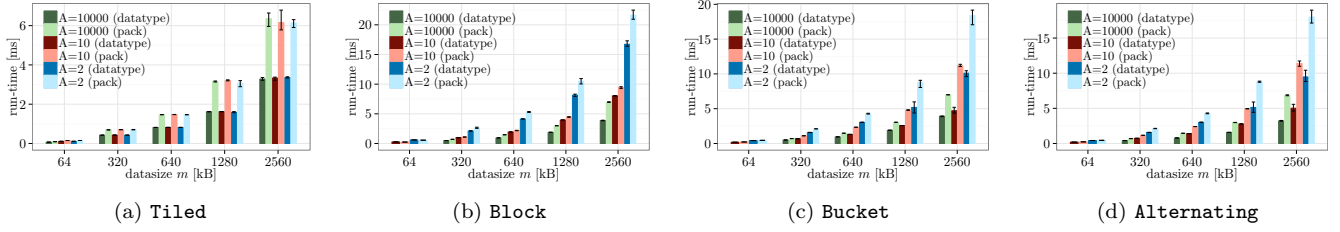


Figure 48: Basic layouts vs. pack/unpack, element datatype: MPI_INT, one node, 2 processes, Ping-pong, NEC MPI-1.3.1.

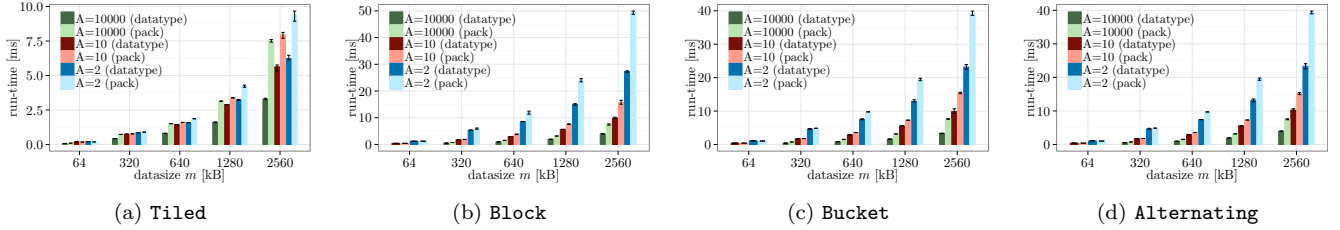


Figure 49: Basic layouts vs. pack/unpack, element datatype: MPI_INT, one node, 2 processes, Ping-pong, MVAPICH2-2.1.

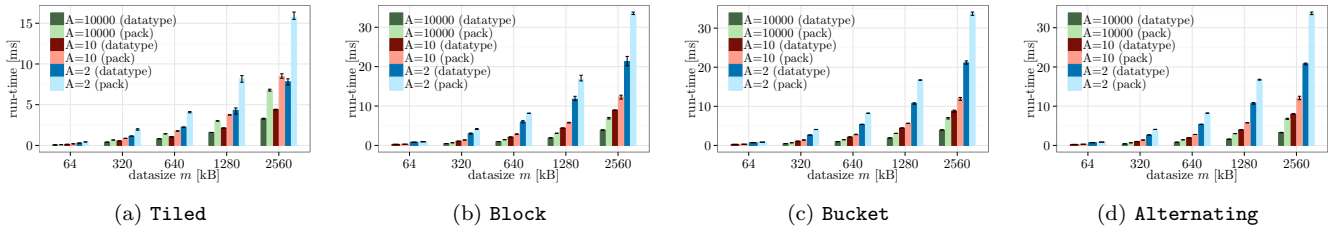


Figure 50: Basic layouts vs. pack/unpack, element datatype: MPI_INT, one node, 2 processes, Ping-pong, OpenMPI-1.10.1.

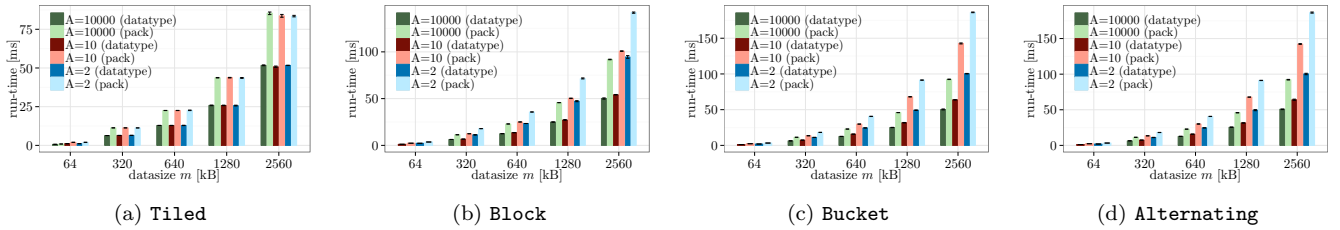


Figure 51: Basic layouts vs. pack/unpack, element datatype: MPI_INT, one node, 16 processes, MPI_Allgather, NEC MPI-1.3.1.

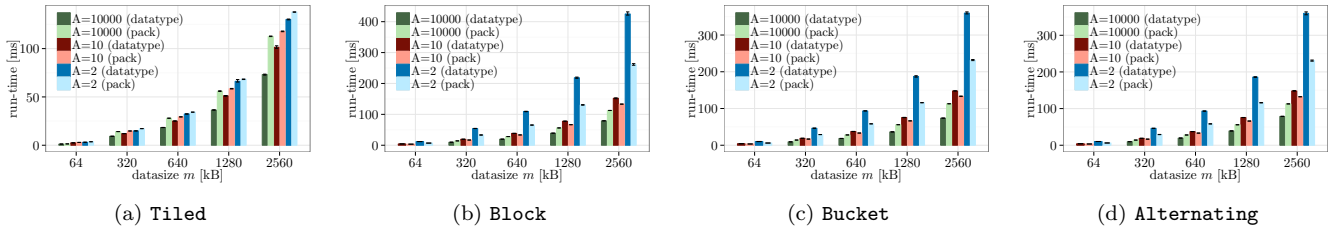


Figure 52: Basic layouts vs. pack/unpack, element datatype: MPI_INT, one node, 16 processes, MPI_Allgather, MVA-PICH2-2.1.

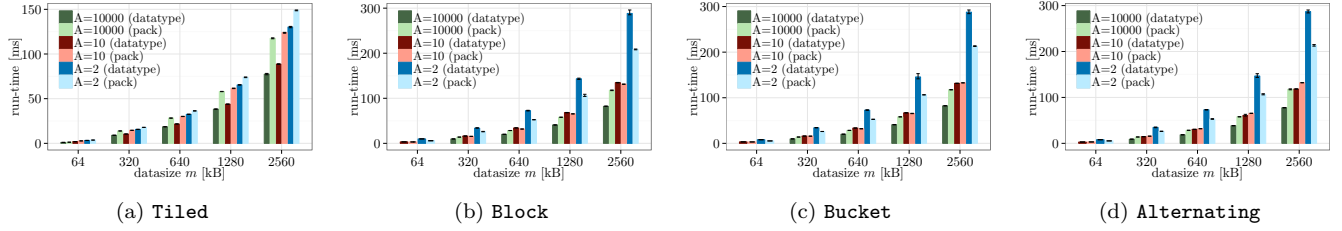


Figure 53: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, one node, 16 processes, `MPI_Allgather`, OpenMPI-1.10.1.

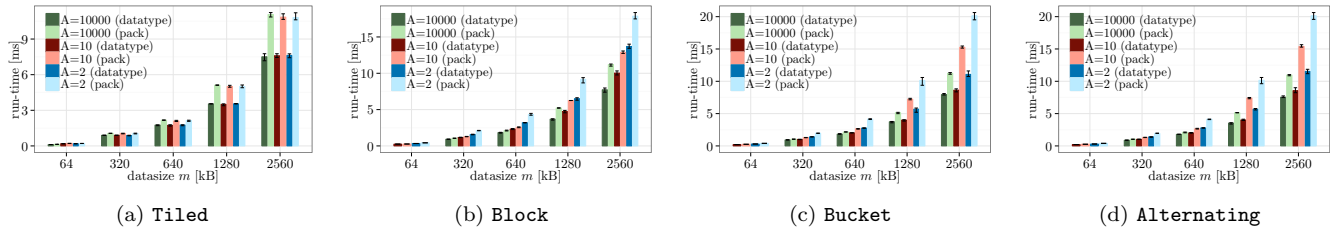


Figure 54: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, one node, 16 processes, `MPI_Bcast`, NEC MPI-1.3.1.

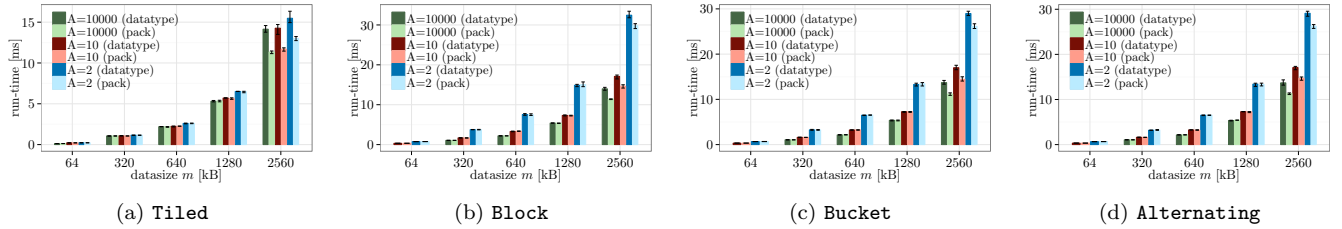


Figure 55: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, one node, 16 processes, `MPI_Bcast`, MVAPICH2-2.1.

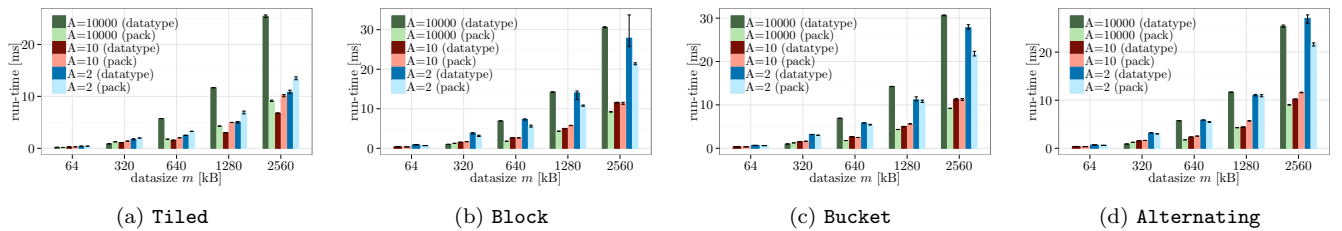


Figure 56: Basic layouts vs. pack/unpack, element datatype: `MPI_INT`, one node, 16 processes, `MPI_Bcast`, OpenMPI-1.10.1.

A.4 Expectation Test 4 (Sect. 3.2.2)

- Contiguous-subtype vs. basic layouts (Tiled, Block, Bucket, Alternating)
- Ping-pong

- Figure 57: NEC MPI-1.3.1, small datasize
- Figure 58: MVAPICH2-2.1, small datasize
- Figure 59: OpenMPI-1.10.1, small datasize
- Figure 60: NEC MPI-1.3.1, large datasize
- Figure 61: MVAPICH2-2.1, large datasize
- Figure 62: OpenMPI-1.10.1, large datasize

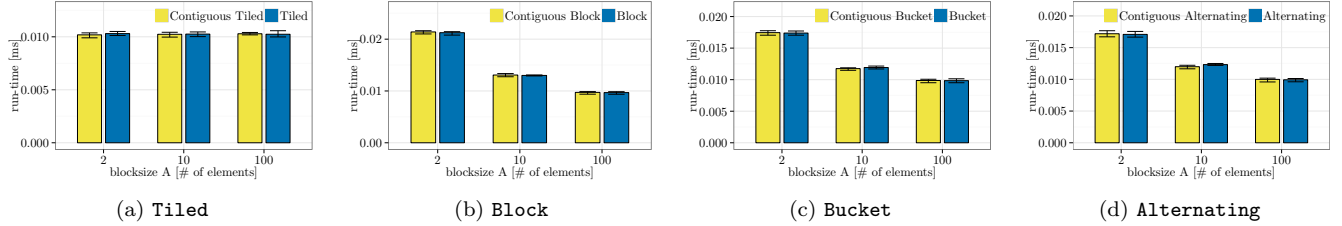


Figure 57: Basic layouts vs. Contiguous-subtype, $m = 2\text{ kBytes}$, element datatype: MPI_INT, 2×1 processes, Ping-pong, NEC MPI-1.3.1 (similar results for 1×2 processes).

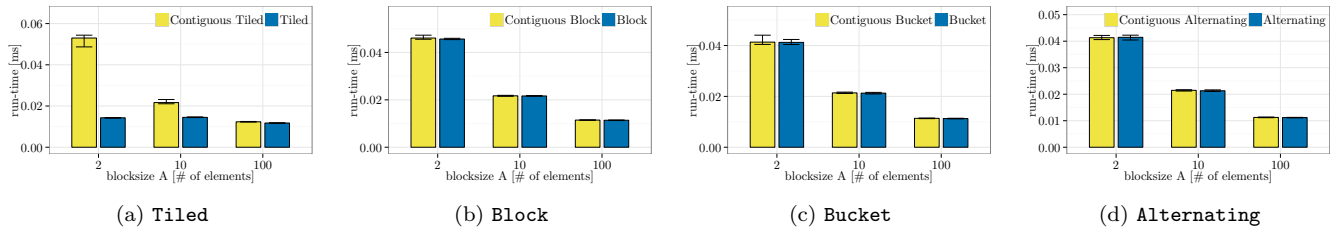


Figure 58: Basic layouts vs. Contiguous-subtype, $m = 2\text{ kBytes}$, element datatype: MPI_INT, 2×1 processes, Ping-pong, MVAPICH2-2.1 (similar results for 1×2 processes).

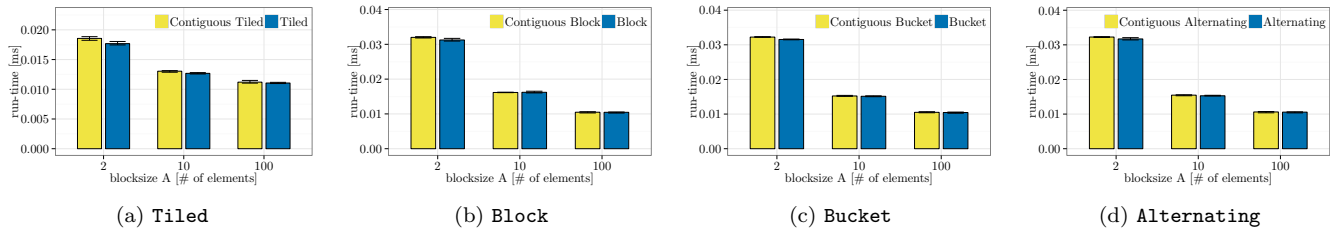


Figure 59: Basic layouts vs. Contiguous-subtype, $m = 2\text{ kBytes}$, element datatype: MPI_INT, 2×1 processes, Ping-pong, OpenMPI-1.10.1 (similar results for 1×2 processes).

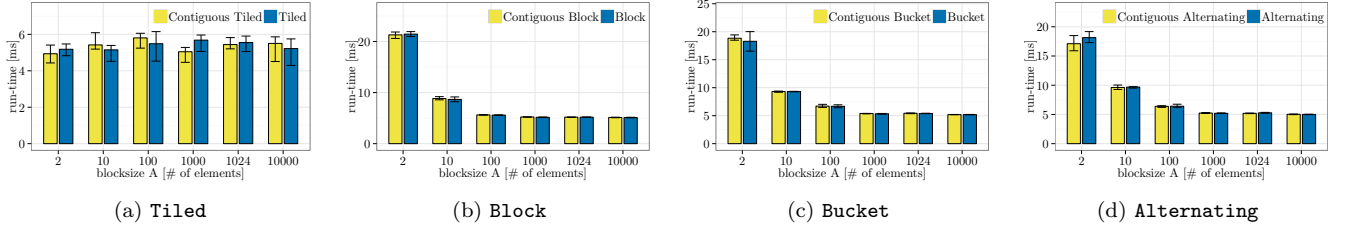


Figure 60: Basic layouts vs. **Contiguous-subtype**, $m = 2.56$ MBytes, element datatype: MPI_INT, 2×1 processes, Ping-pong, NEC MPI-1.3.1 (similar results for 1×2 processes).

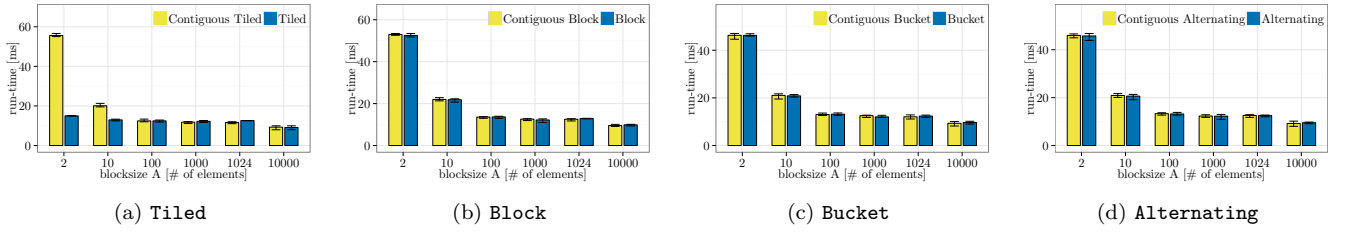


Figure 61: Basic layouts vs. **Contiguous-subtype**, $m = 2.56$ MBytes, element datatype: MPI_INT, 2×1 processes, Ping-pong, MVAPICH2-2.1 (similar results for 1×2 processes).

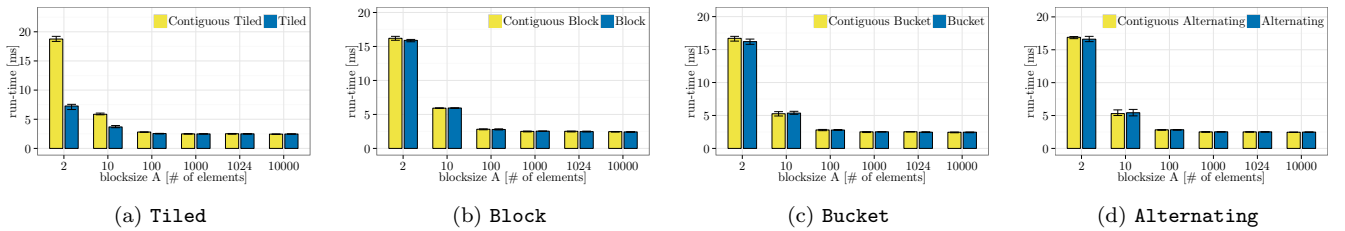
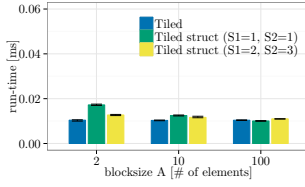


Figure 62: Basic layouts vs. **Contiguous-subtype**, $m = 2.56$ MBytes, element datatype: MPI_INT, 2×1 processes, Ping-pong, OpenMPI-1.10.1 (similar results for 1×2 processes).

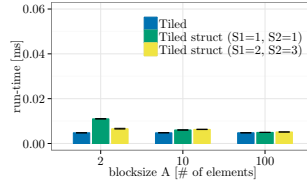
A.5 Expectation Test 5 (Sect. 3.2.3)

- Tiled (AB), Tiled-struct
- Ping-pong

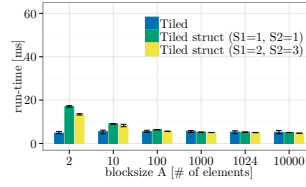
- Figure 63: NEC MPI-1.3.1
- Figure 64: MVAPICH2-2.1
- Figure 65: OpenMPI-1.10.1



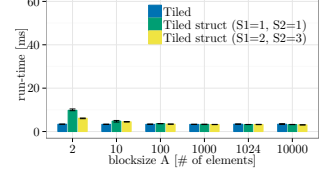
(a) $m = 2 \text{ kBytes}$, 2 nodes



(b) $m = 2 \text{ kBytes}$, same node

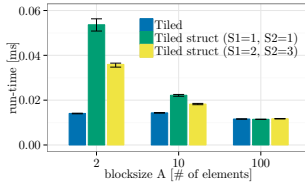


(c) $m = 2.56 \text{ MBytes}$, 2 nodes

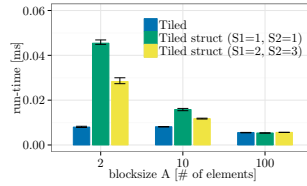


(d) $m = 2.56 \text{ MBytes}$, same node

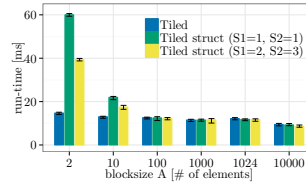
Figure 63: Tiled (AB) vs. Tiled-struct, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.



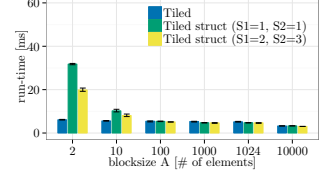
(a) $m = 2 \text{ kBytes}$, 2 nodes



(b) $m = 2 \text{ kBytes}$, same node

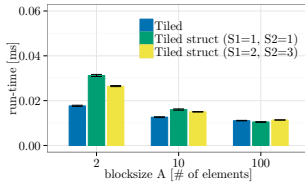


(c) $m = 2.56 \text{ MBytes}$, 2 nodes

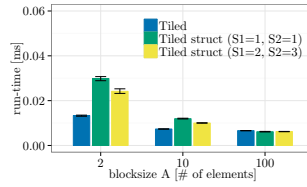


(d) $m = 2.56 \text{ MBytes}$, same node

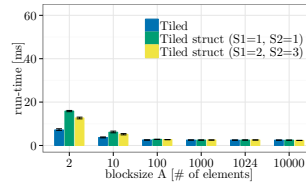
Figure 64: Tiled (AB) vs. Tiled-struct, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.



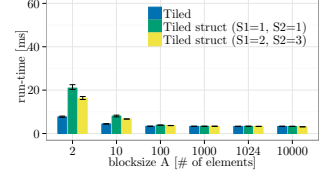
(a) $m = 2 \text{ kBytes}$, 2 nodes



(b) $m = 2 \text{ kBytes}$, same node



(c) $m = 2.56 \text{ MBytes}$, 2 nodes



(d) $m = 2.56 \text{ MBytes}$, same node

Figure 65: Tiled (AB) vs. Tiled-struct, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

A.6 Expectation Test 6 (Sect. 3.2.4)

- Tiled (AB), Tiled-vector
- Ping-pong
- Figure 66: NEC MPI-1.3.1
- Figure 67: MVAPICH2-2.1
- Figure 68: OpenMPI-1.10.1

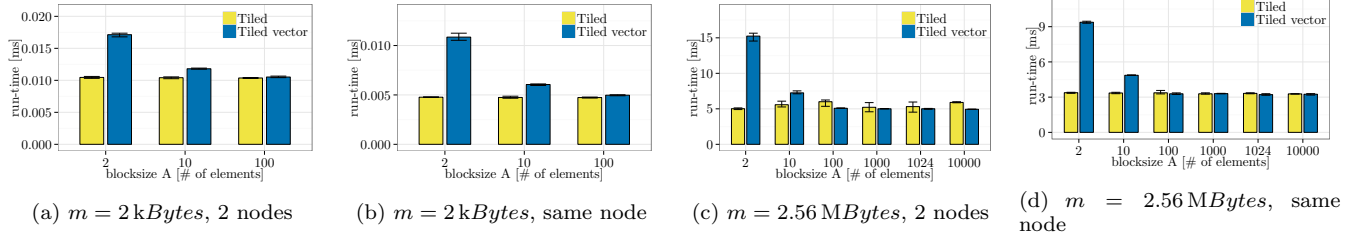


Figure 66: Tiled (AB) vs. Tiled-vector, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.

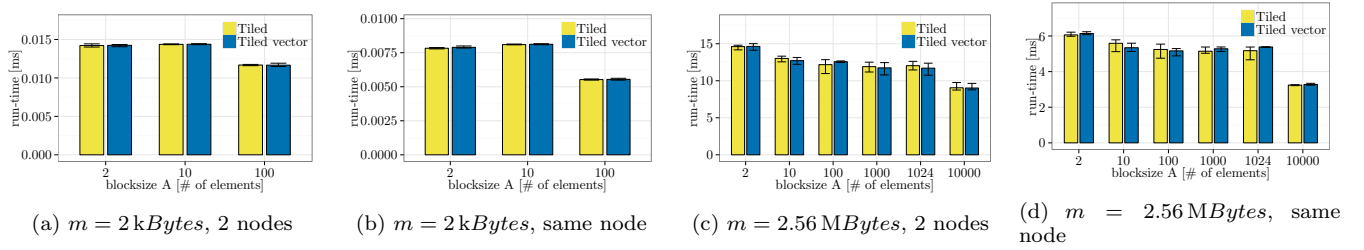


Figure 67: Tiled (AB) vs. Tiled-vector, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.

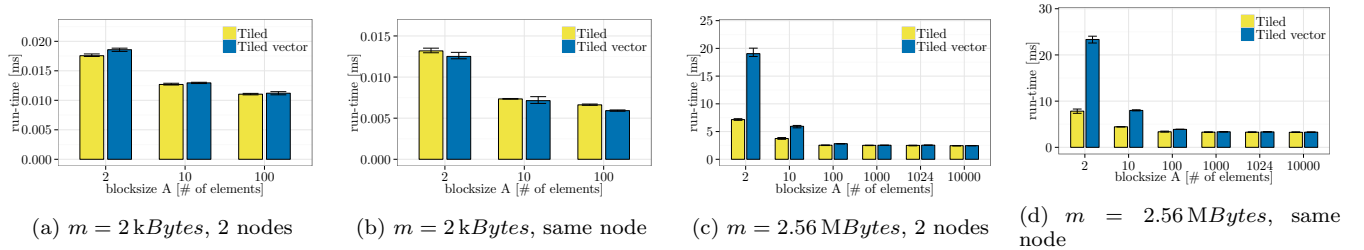
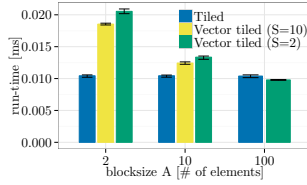


Figure 68: Tiled (AB) vs. Tiled-vector, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

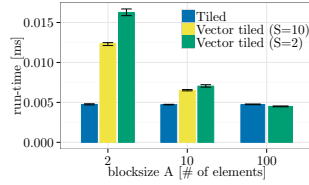
A.7 Expectation Test 7 (Sect. 3.2.5)

- Tiled (AB), Vector-tiled
- Ping-pong

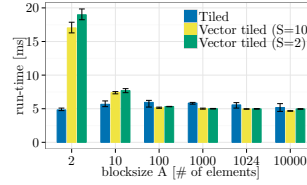
- Figure 69: NEC MPI-1.3.1
- Figure 70: MVAPICH2-2.1
- Figure 71: OpenMPI-1.10.1



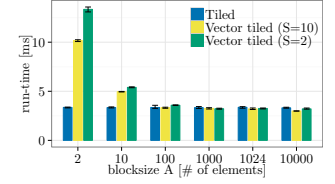
(a) $m = 2 \text{ kBytes}$, 2 nodes



(b) $m = 2 \text{ kBytes}$, same node

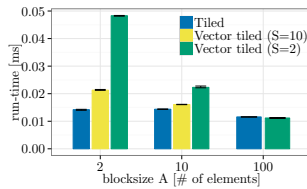


(c) $m = 2.56 \text{ MBytes}$, 2 nodes

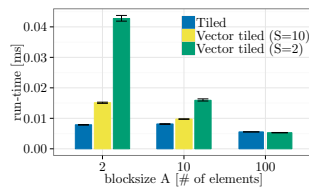


(d) $m = 2.56 \text{ MBytes}$, same node

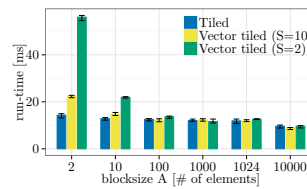
Figure 69: Tiled (AB) vs. Vector-tiled, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.



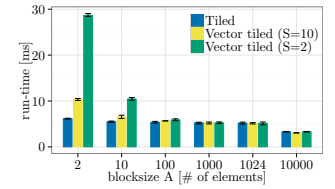
(a) $m = 2 \text{ kBytes}$, 2 nodes



(b) $m = 2 \text{ kBytes}$, same node

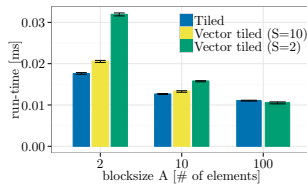


(c) $m = 2.56 \text{ MBytes}$, 2 nodes

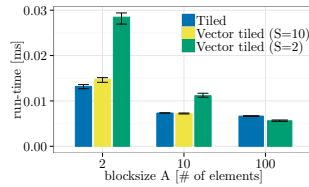


(d) $m = 2.56 \text{ MBytes}$, same node

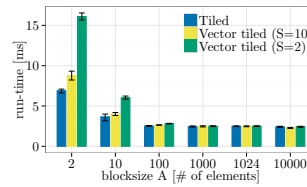
Figure 70: Tiled (AB) vs. Vector-tiled, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.



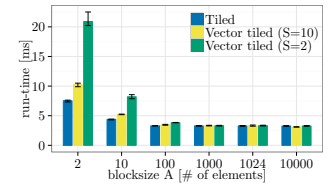
(a) $m = 2 \text{ kBytes}$, 2 nodes



(b) $m = 2 \text{ kBytes}$, same node



(c) $m = 2.56 \text{ MBytes}$, 2 nodes



(d) $m = 2.56 \text{ MBytes}$, same node

Figure 71: Tiled (AB) vs. Vector-tiled, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

A.8 Expectation Test 8 (Sect. 3.2.6)

- Block, Block-indexed
 - Ping-pong
-
- Figure 72: NEC MPI-1.3.1
 - Figure 73: MVAPICH2-2.1
 - Figure 74: OpenMPI-1.10.1
-

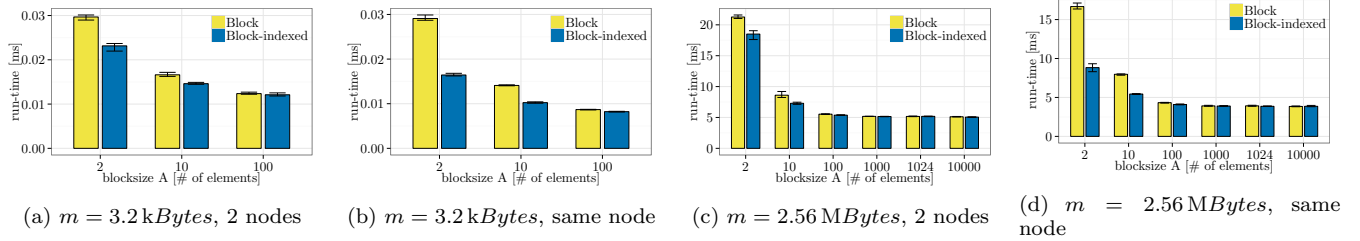


Figure 72: Block vs. Block-indexed, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.

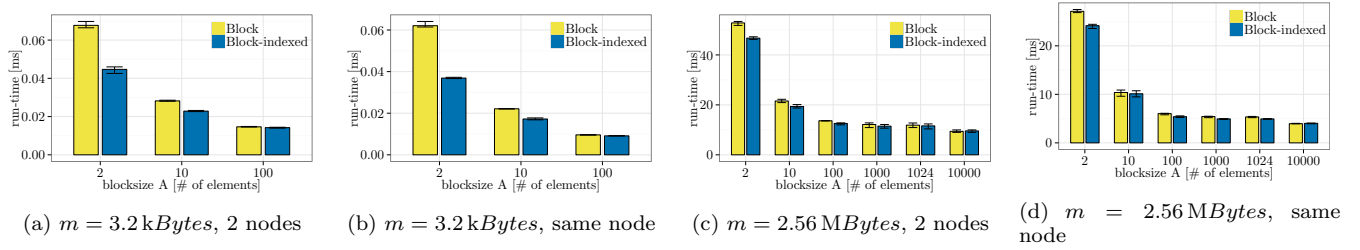


Figure 73: Block vs. Block-indexed, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.

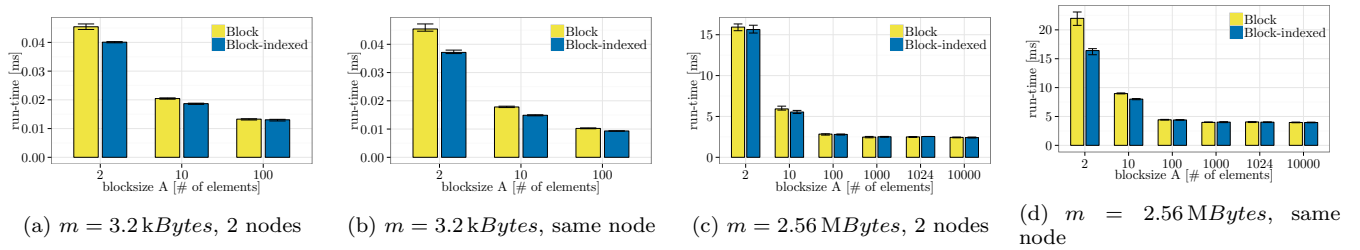


Figure 74: Block vs. Block-indexed, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

A.9 Expectation Test 9 (Sect. 3.2.7)

- Alternating, Alternating-indexed
- Ping-pong

- Figure 75: NEC MPI-1.3.1
- Figure 76: MVAPICH2-2.1
- Figure 77: OpenMPI-1.10.1

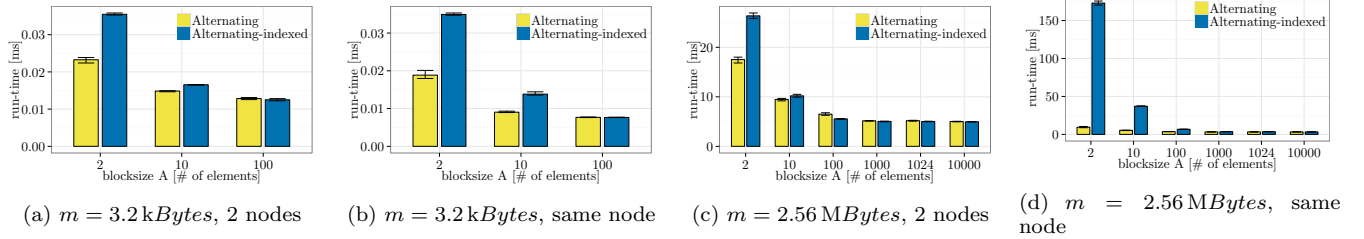


Figure 75: Alternating vs. Alternating-indexed, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.

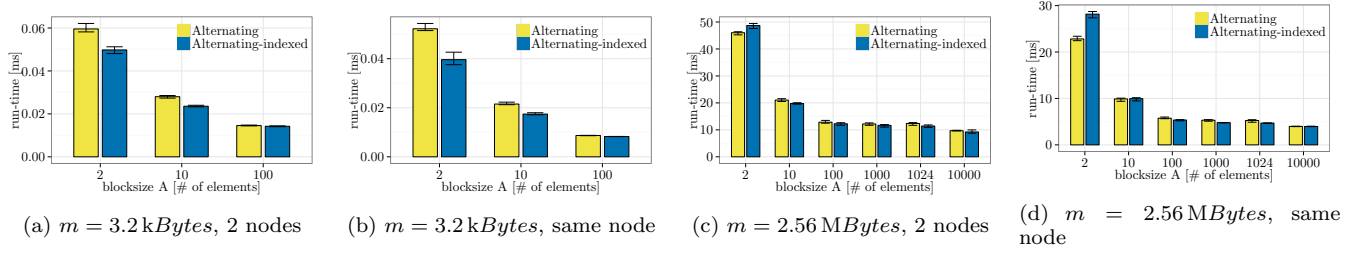


Figure 76: Alternating vs. Alternating-indexed, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.

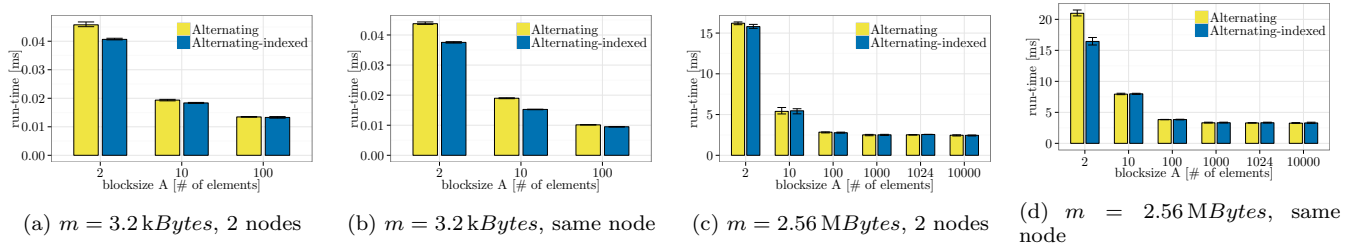


Figure 77: Alternating vs. Alternating-indexed, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

A.10 Expectation Test 10 (Sect. 3.2.8)

- Alternating-repeated, Alternating-struct
- Ping-pong

- Figure 78: NEC MPI-1.3.1
- Figure 79: MVAPICH2-2.1
- Figure 80: OpenMPI-1.10.1

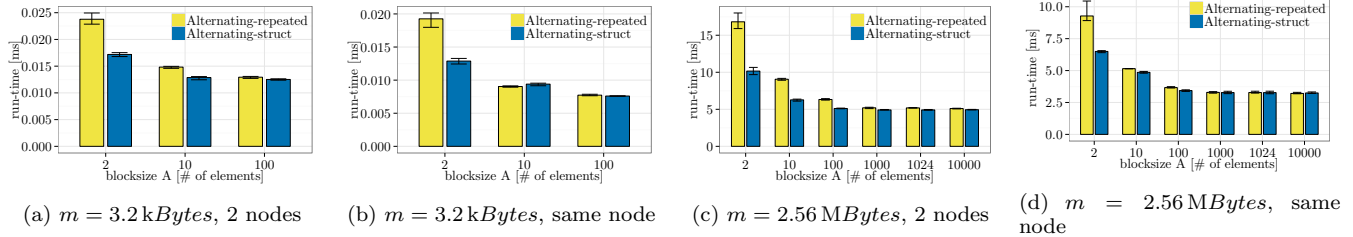


Figure 78: Alternating-repeated vs. Alternating-struct, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.

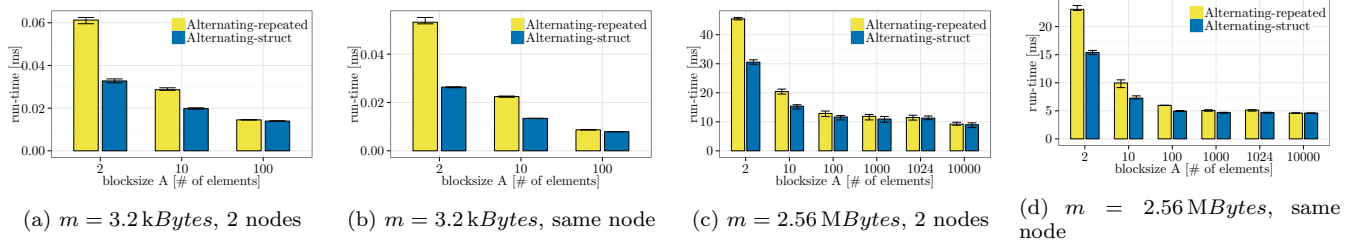


Figure 79: Alternating-repeated vs. Alternating-struct, element datatype: MPI_INT, Ping-pong, MVAPICH2-2.1.

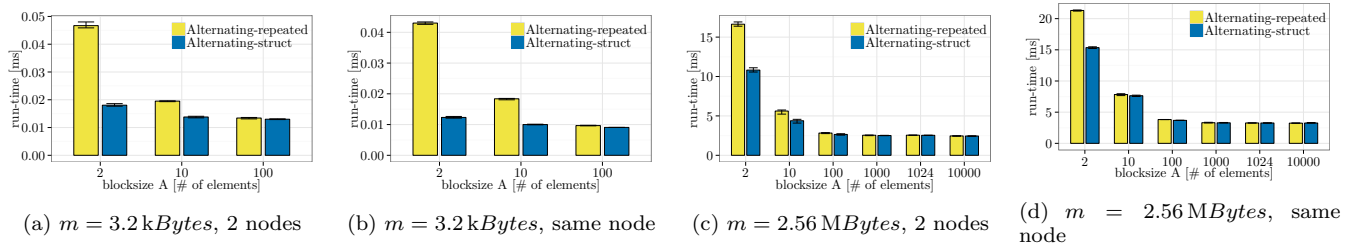


Figure 80: Alternating-repeated vs. Alternating-struct, element datatype: MPI_INT, Ping-pong, OpenMPI-1.10.1.

A.11 Expectation Test 11 (Sect. 3.2.9)

- RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct
- Ping-pong
- Figure 81: NEC MPI-1.3.1
- Figure 82: MVAPICH2-2.1
- Figure 83: OpenMPI-1.10.1

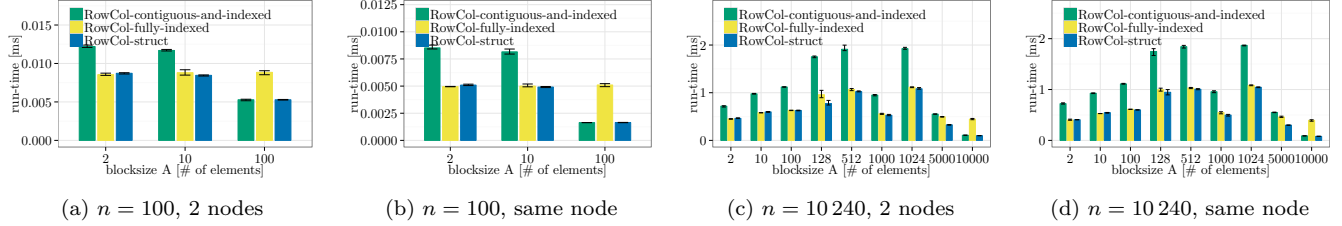


Figure 81: RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct, element datatype: MPI_INT, buffer size (and extent) increases with blocksize A, Ping-pong, NEC MPI-1.3.1.

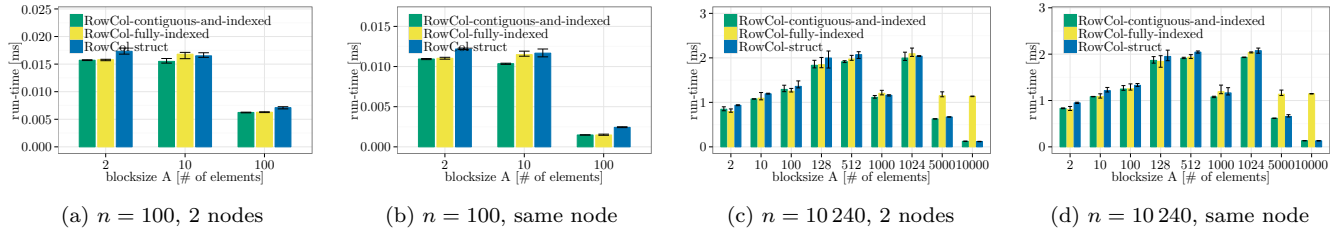


Figure 82: RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct, element datatype: MPI_INT, buffer size (and extent) increases with blocksize A, Ping-pong, MVAPICH2-2.1.

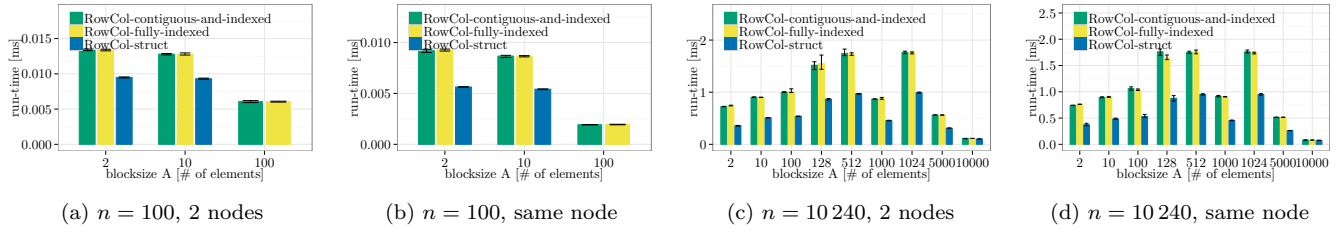


Figure 83: RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct, element datatype: MPI_INT, buffer size (and extent) increases with blocksize A, Ping-pong, OpenMPI-1.10.1.

B. EXPERIMENTAL RESULTS ON VSC-3

The experiments in this appendix have been performed using the hardware and software setup described below:

machine	2000 × Dual Intel Xeon E5-2650v2 @ 2.6 GHz
	InfiniBand QDR-80
machine name	VSC-3
MPI libraries	Intel MPI-5.1.3
Compiler	Intel 16.0.1 (flags -O3)

B.1 Expectation Test 1 (Sect. 2.4.1)

- Contiguous, Tiled (AB), Block ($\bar{A}\bar{B}$), Bucket ($\bar{A}B$), Alternating ($\bar{A}\bar{B}$)
- Ping-pong, MPI_Bcast, MPI_Allgather

- Figure 84: Intel MPI-5.1.3, small datasize, **Variant 1**
- Figure 85: Intel MPI-5.1.3, large datasize, **Variant 1**
- Figure 86: Intel MPI-5.1.3, small datasize, **Variant 1**, one node
- Figure 87: Intel MPI-5.1.3, large datasize, **Variant 1**, one node
- Figure 88: Intel MPI-5.1.3, small datasize, **Variant 2**
- Figure 89: Intel MPI-5.1.3, large datasize, **Variant 2**
- Figure 90: Intel MPI-5.1.3, small datasize, **Variant 2**, one node
- Figure 91: Intel MPI-5.1.3, large datasize, **Variant 2**, one node

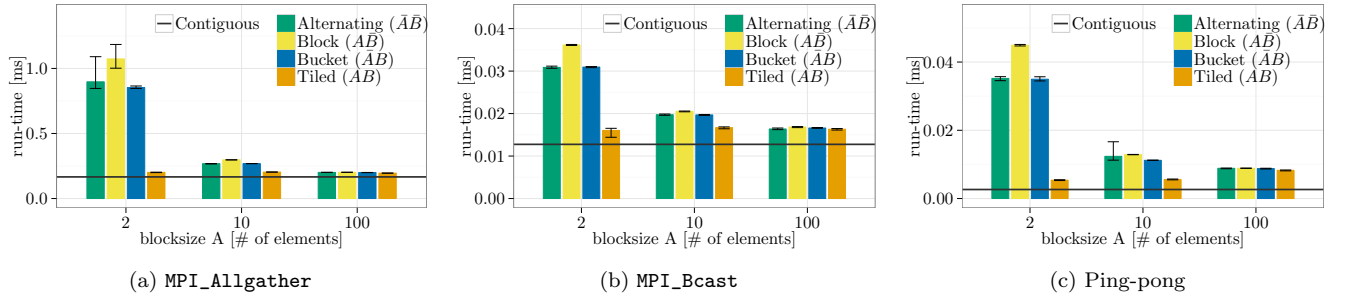


Figure 84: Contiguous vs. typed, $m = 3.2kBytes$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), Intel MPI-5.1.3, **Variant 1**.

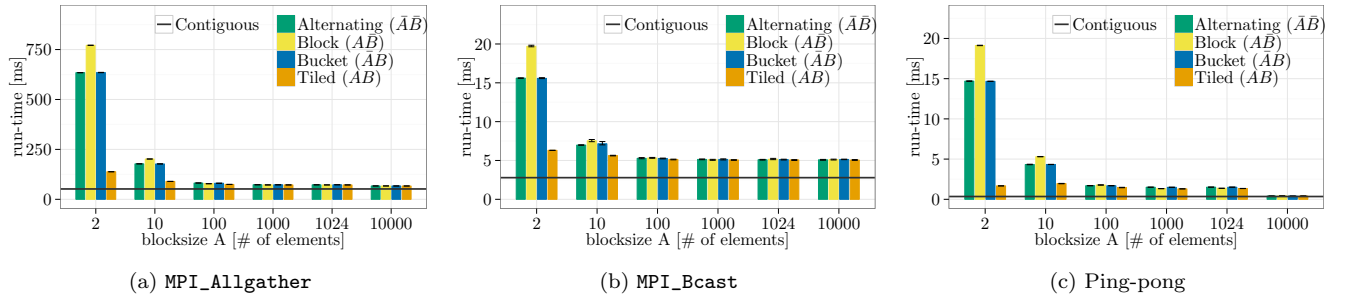


Figure 85: Contiguous vs. typed, $m = 2.56 MBytes$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), Intel MPI-5.1.3, **Variant 1**.

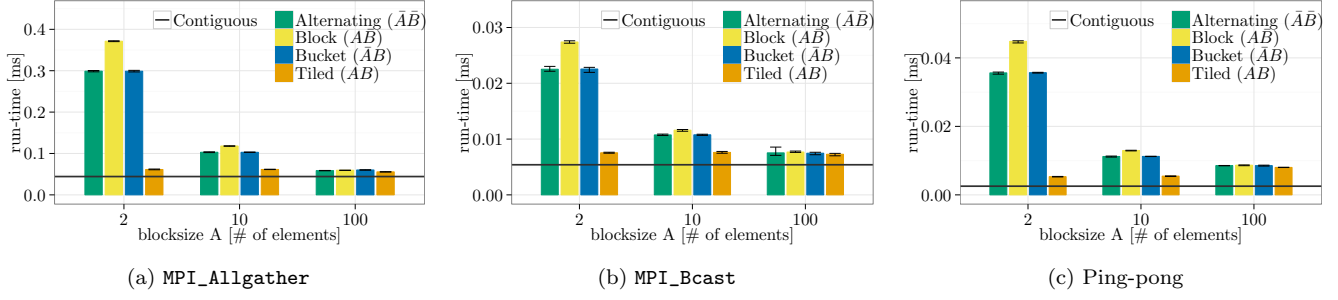


Figure 86: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, one node, 16 processes (2 for Ping-pong), Intel MPI-5.1.3, **Variant 1**.

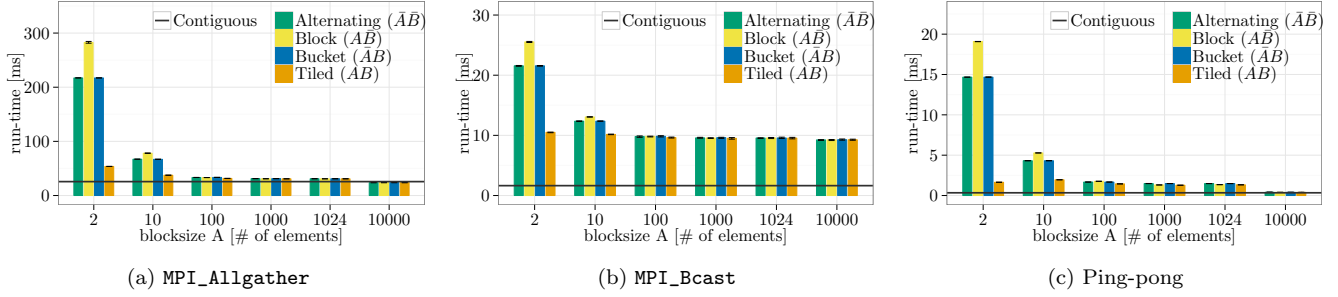


Figure 87: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, one node, 16 processes (2 processes for Ping-pong), Intel MPI-5.1.3, **Variant 1**.

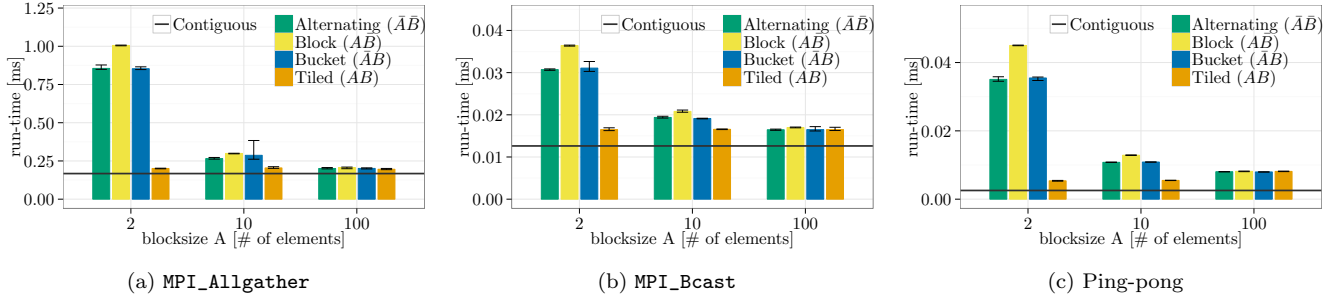


Figure 88: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), Intel MPI-5.1.3, **Variant 2**.

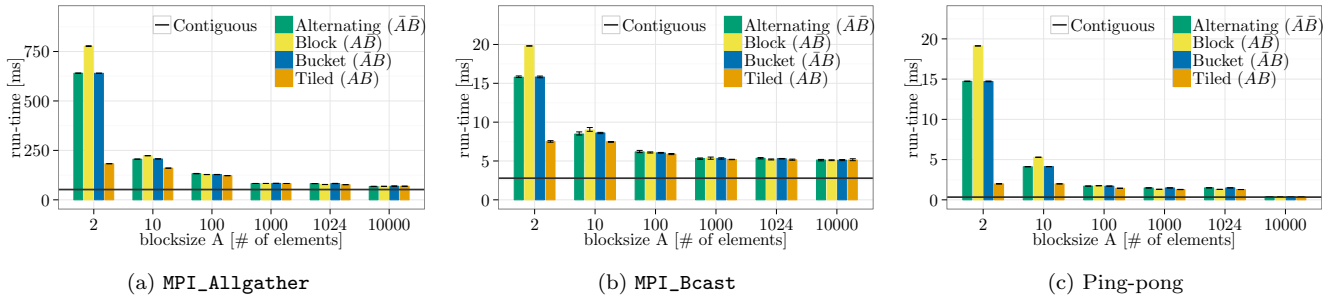


Figure 89: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: MPI_INT, 32×1 processes (2×1 for Ping-pong), Intel MPI-5.1.3, **Variant 2**.

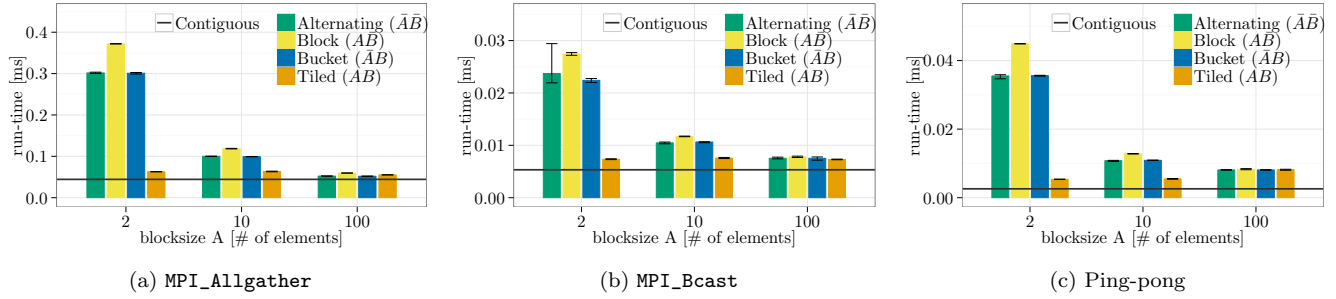


Figure 90: Contiguous vs. typed, $m = 3.2\text{kBytes}$, element datatype: `MPI_INT`, one node, 16 processes (2 for Ping-pong), Intel MPI-5.1.3, **Variant 2**.

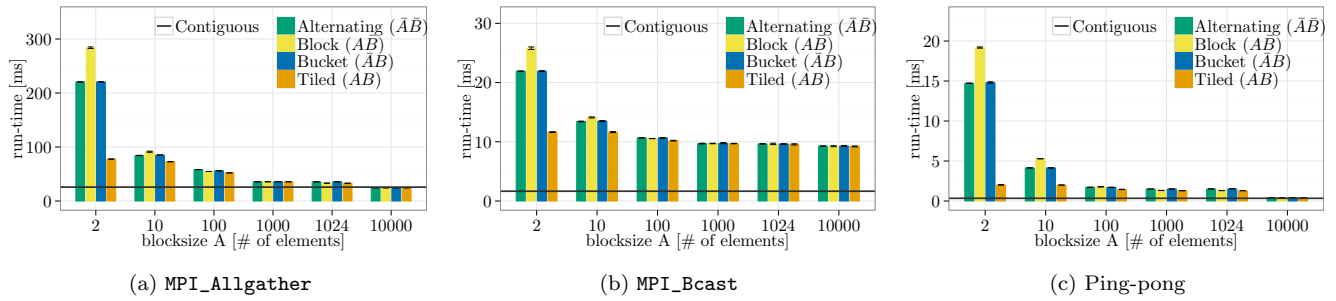


Figure 91: Contiguous vs. typed, $m = 2.56\text{MBytes}$, element datatype: `MPI_INT`, one node, 16 processes (2 for Ping-pong), Intel MPI-5.1.3, **Variant 2**.

B.2 Expectation Test 2 (Sect. 2.4.2)

- Contiguous, Tiled-heterogeneous ($AB\bar{T}$)
- Ping-pong
- Figure 92: Intel MPI-5.1.3

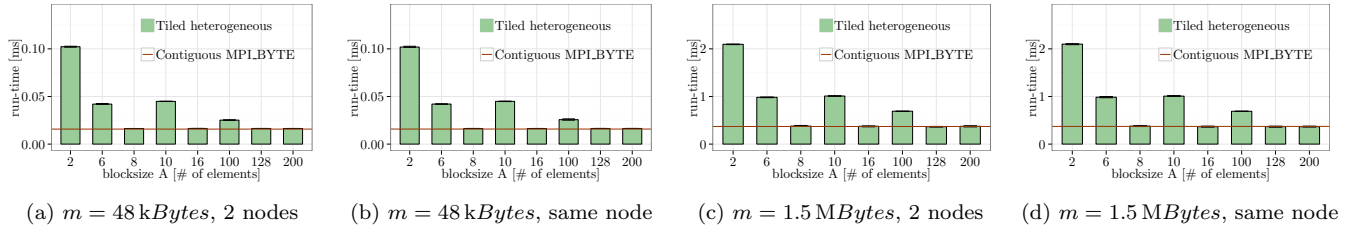


Figure 92: Contiguous vs. Tiled-heterogeneous ($AB\bar{T}$) $A=B$, element datatype: `MPI_INT`, Ping-pong, Intel MPI-5.1.3.

B.3 Expectation Test 3 (Sect. 3.2.1)

- pack vs. unpack for basic layouts (Tiled, Block, Bucket, Alternating)
- MPI_Allgather, MPI_Bcast, Ping-pong
- Figure 93: Intel MPI-5.1.3, Ping-pong, 2×1 processes
- Figure 94: Intel MPI-5.1.3, Ping-pong, one node, 2 processes

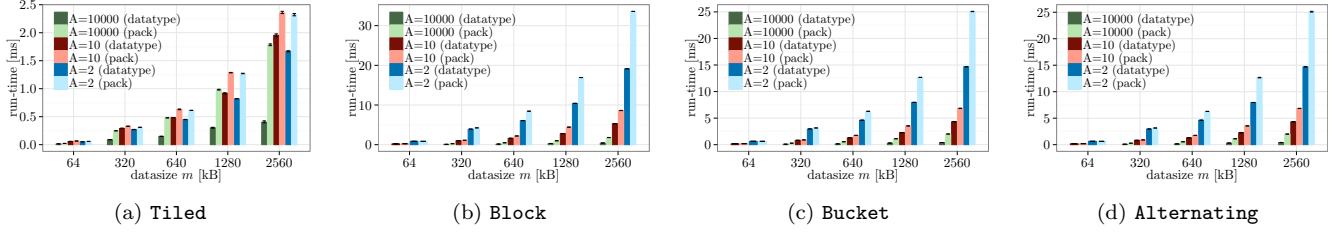


Figure 93: Basic layouts vs. pack/unpack, element datatype: MPI_INT, 2×1 processes, Ping-pong, Intel MPI-5.1.3.

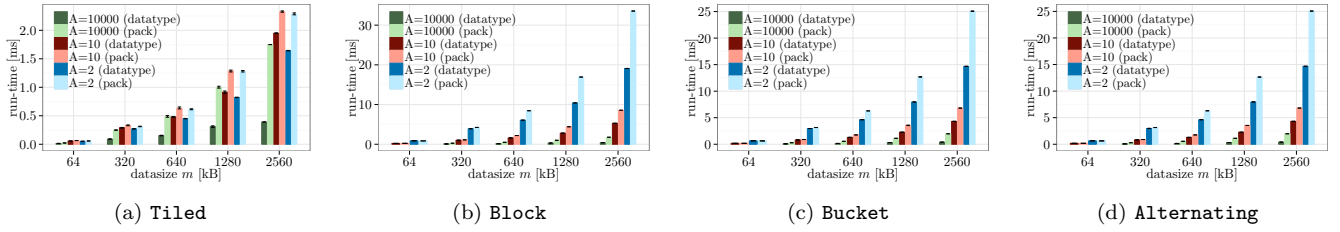


Figure 94: Basic layouts vs. pack/unpack, element datatype: MPI_INT, one node, 2 processes, Ping-pong, Intel MPI-5.1.3.

B.4 Expectation Test 4 (Sect. 3.2.2)

- Contiguous-subtype vs. basic layouts (Tiled, Block, Bucket, Alternating)
- Ping-pong, MPI_Allgather, MPI_Bcast

- Figure 95: Intel MPI-5.1.3, Ping-pong, small datasize
- Figure 96: Intel MPI-5.1.3, Ping-pong, large datasize
- Figure 97: Intel MPI-5.1.3, MPI_Allgather, small datasize
- Figure 98: Intel MPI-5.1.3, MPI_Allgather, large datasize
- Figure 99: Intel MPI-5.1.3, MPI_Bcast, small datasize
- Figure 100: Intel MPI-5.1.3, MPI_Bcast, large datasize

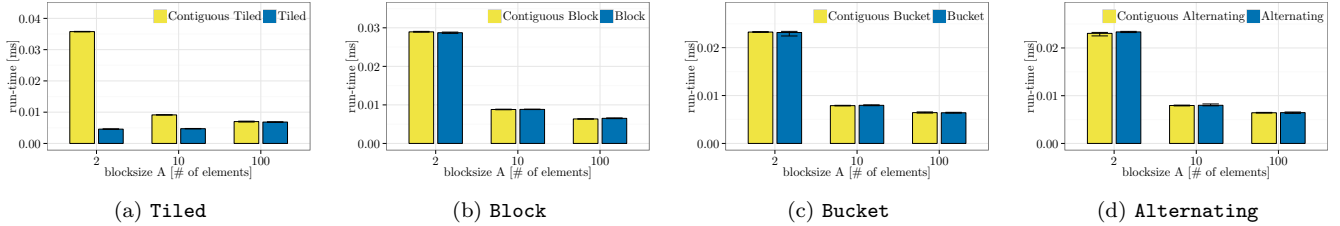


Figure 95: Basic layouts vs. Contiguous-subtype, $m = 2 \text{ kBytes}$, element datatype: MPI_INT, 2×1 processes, Ping-pong, Intel MPI-5.1.3 (similar results for 1×2 processes).

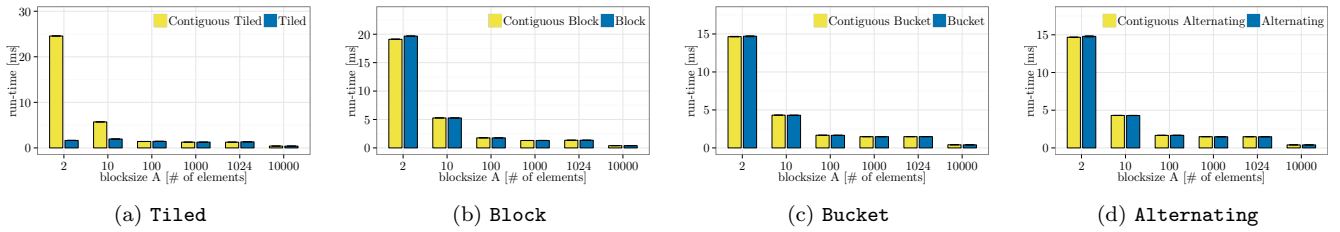


Figure 96: Basic layouts vs. Contiguous-subtype, $m = 2.56 \text{ MBytes}$, element datatype: MPI_INT, 2×1 processes, Ping-pong, Intel MPI-5.1.3 (similar results for 1×2 processes).

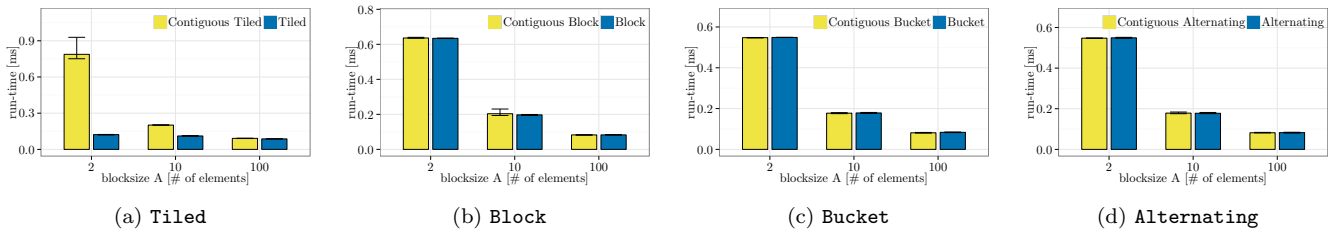


Figure 97: Basic layouts vs. Contiguous-subtype, $m = 2 \text{ kBytes}$, element datatype: MPI_INT, 32×1 processes, MPI_Allgather, Intel MPI-5.1.3 (similar results for 1×16 processes).

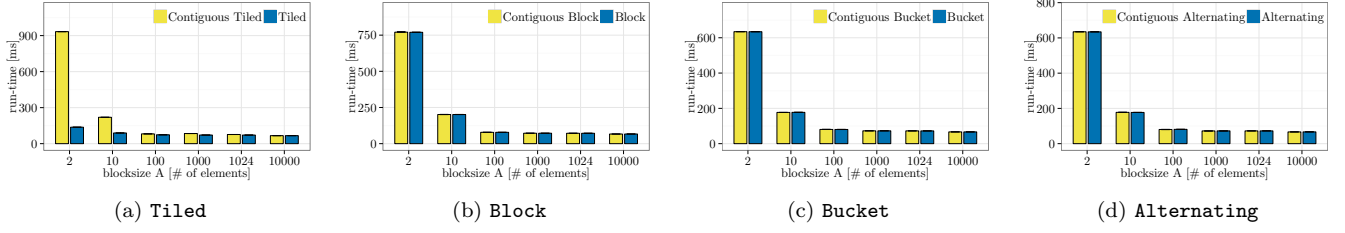


Figure 98: Basic layouts vs. **Contiguous-subtype**, $m = 2.56$ MBytes, element datatype: MPI_INT, 32×1 processes, MPI_Allgather, Intel MPI-5.1.3 (similar results for 1×16 processes).

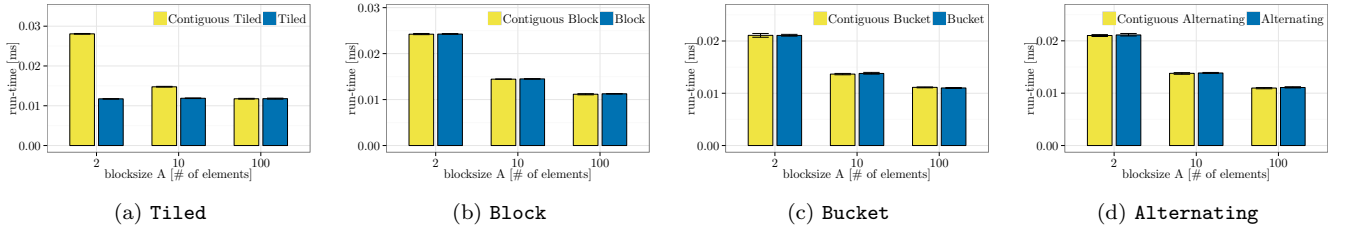


Figure 99: Basic layouts vs. **Contiguous-subtype**, $m = 2$ kBytes, element datatype: MPI_INT, 32×1 processes, MPI_Bcast, Intel MPI-5.1.3 (similar results for 1×16 processes).

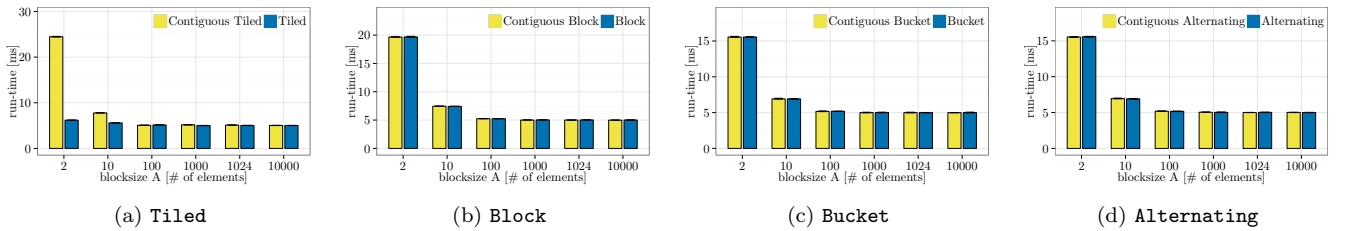
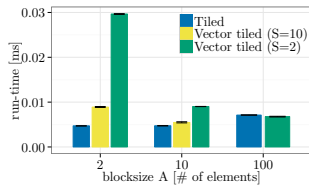


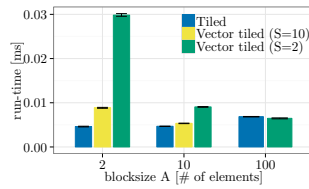
Figure 100: Basic layouts vs. **Contiguous-subtype**, $m = 2.56$ MBytes, element datatype: MPI_INT, 32×1 processes, MPI_Bcast, Intel MPI-5.1.3 (similar results for 1×16 processes).

B.5 Expectation Test 7 (Sect. 3.2.5)

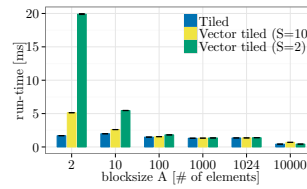
- Tiled (AB), Vector-tiled
- Ping-pong
- Figure 101: Intel MPI-5.1.3



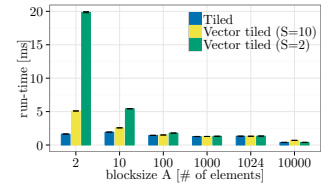
(a) $m = 2\text{ kBytes}$, 2 nodes



(b) $m = 2\text{ kBytes}$, same node



(c) $m = 2.56\text{ MBytes}$, 2 nodes

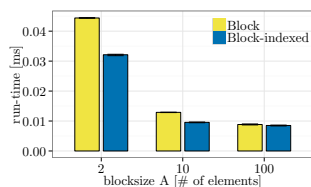


(d) $m = 2.56\text{ MBytes}$, same node

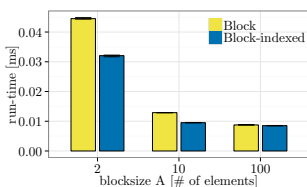
Figure 101: Tiled (AB) vs. Vector-tiled, element datatype: `MPI_INT`, Ping-pong, Intel MPI-5.1.3.

B.6 Expectation Test 8 (Sect. 3.2.6)

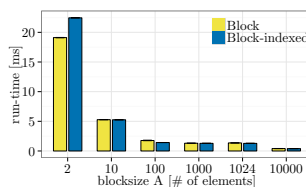
- Block, Block-indexed
- Ping-pong
- Figure 102: Intel MPI-5.1.3



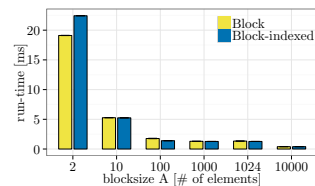
(a) $m = 3.2 \text{ kBytes}$, 2 nodes



(b) $m = 3.2 \text{ kBytes}$, same node



(c) $m = 2.56 \text{ MBytes}$, 2 nodes



(d) $m = 2.56 \text{ MBytes}$, same node

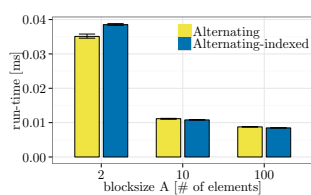
Figure 102: Block vs. Block-indexed, element datatype: MPI_INT, Ping-pong, Intel MPI-5.1.3.

B.7 Expectation Test 9 (Sect. 3.2.7)

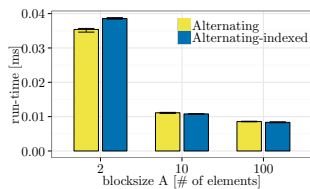
· Alternating, Alternating-indexed

· Ping-pong

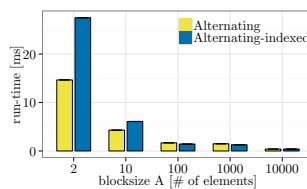
· Figure 103: Intel MPI-5.1.3



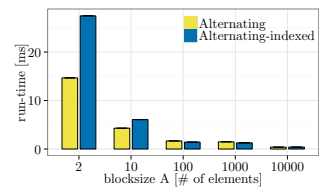
(a) $m = 3.2 \text{ kBytes}$, 2 nodes



(b) $m = 3.2 \text{ kBytes}$, same node



(c) $m = 2.56 \text{ MBytes}$, 2 nodes



(d) $m = 2.56 \text{ MBytes}$, same node

Figure 103: Alternating vs. Alternating-indexed, element datatype: MPI_INT, Ping-pong, NEC MPI-1.3.1.

B.8 Expectation Test 10 (Sect. 3.2.8)

· Alternating-repeated, Alternating-struct

· Ping-pong

· Figure 104: Intel MPI-5.1.3

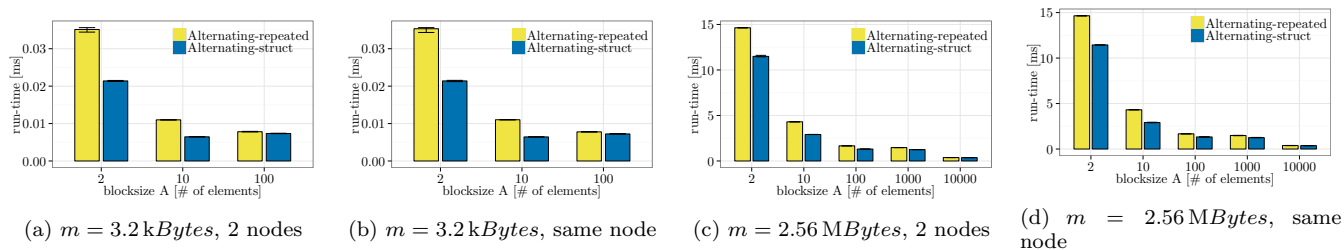


Figure 104: Alternating-repeated vs. Alternating-struct, element datatype: MPI_INT, Ping-pong, Intel MPI-5.1.3.

B.9 Expectation Test 5 (Sect. 3.2.3)

- Tiled (AB), Tiled-struct
 - Ping-pong
-
- Figure 105: Intel MPI-5.1.3
-

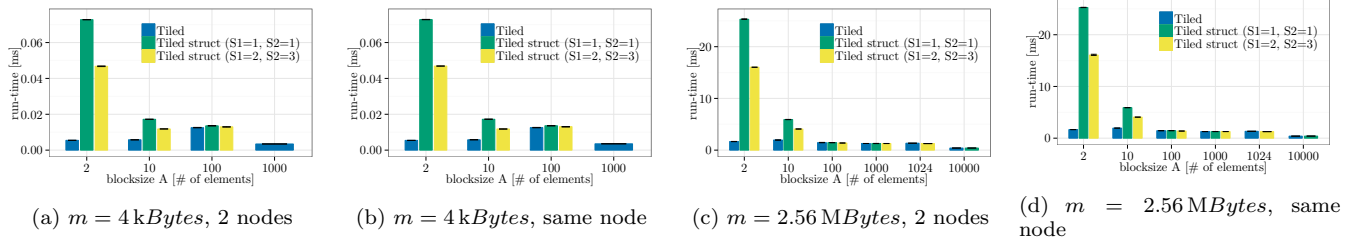


Figure 105: Tiled (AB) vs. Tiled-struct, element datatype: `MPI_INT`, Ping-pong, Intel MPI-5.1.3.

B.10 Expectation Test 6 (Sect. 3.2.4)

- Tiled (AB), Tiled-vector
 - Ping-pong
- Figure 106: Intel MPI-5.1.3

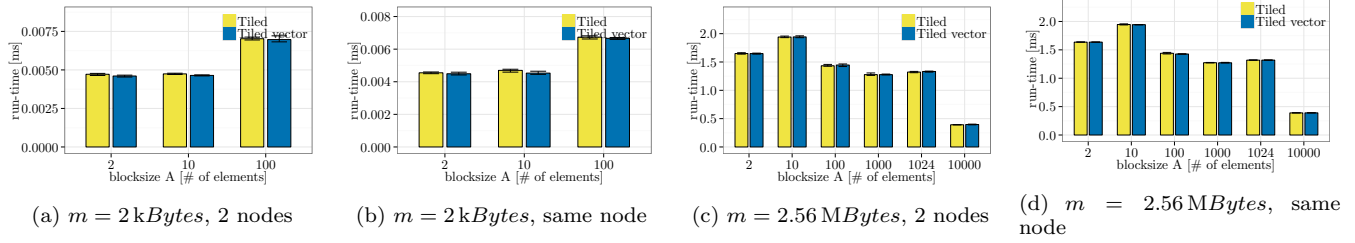


Figure 106: Tiled (AB) vs. Tiled-vector, element datatype: `MPI_INT`, Ping-pong, Intel MPI-5.1.3.

B.11 Expectation Test 11 (Sect. 3.2.9)

- RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct
- Ping-pong
- Figure 107: Intel MPI-5.1.3

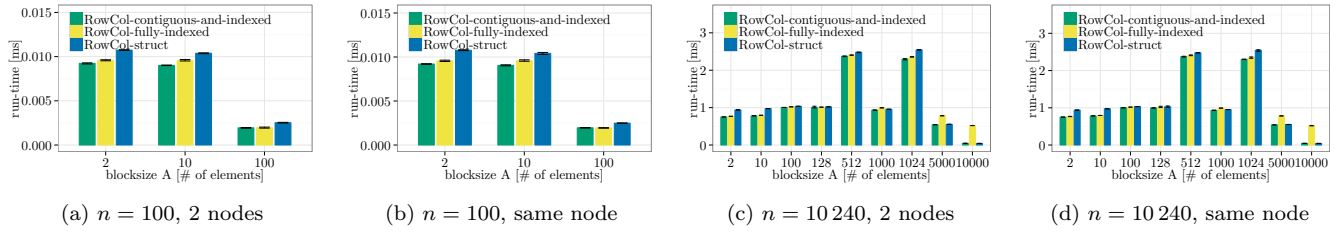


Figure 107: RowCol-fully-indexed, RowCol-contiguous-and-indexed, RowCol-struct, element datatype: MPI_INT, extent increases with blocksize A , Ping-pong, Intel MPI-5.1.3.